Abstract—In interventional cardiology three-dimensional anatomical and functional information of the cardiac chambers would have an important impact on diagnosis and therapy. With the technology of C-arm CT it is possible to reconstruct intraprocedural 3-D images from angiographic projection data. In order to generate accurate and artifact-free reconstructions from dynamic cardiac projections, the motion needs to be taken into account. We present the novel Combined Multiple Heart Phase Registration (CMHPR) method. CMHPR is an iterative motion estimation and compensation algorithm that uses projection data acquired during a single C-arm sweep. Filtered-backprojection (FBP) volumes from electrocardiogram (ECG)-gated data are reconstructed for different motion states of the heart. According to an unknown 4-D motion vector field the ECG-gated FBP images are deformed and accumulated to a sum volume for representing the status of a particular heart phase. In an iterative optimization procedure the 4-D motion vector field is computed by registering the sum volume to a reference volume of the same heart phase. The negative normalized cross correlation (NCC) of both volumes is used as a cost function. In this paper, the reference image is generated using the prior image constrained compressed sensing (PICCS) algorithm combined with the improved total variation (iTV). First preliminary experiments on clinical porcine data sets show promising results. CMHPR reduces streak artifacts and simultaneously preserves sharp edges without producing the artificial comic-like appearance of the PICCS + iTV reference volume.

I. INTRODUCTION

A. Purpose of This Work

In the daily clinical routine, characteristic parameters quantifying the ventricular heart wall motion are based on 2-D angiographic projections acquired with a C-arm system [1]. These images can be used for visual guidance during interventions and to analyze clinically significant parameters, e.g., ejection fraction and wall motion of the heart chambers. Due to the nature of the projection, the images cannot exhibit the status of a particular heart phase. In an iterative optimization procedure the 4-D motion vector field is computed by registering the sum volume to a reference volume of the same heart phase. The negative normalized cross correlation (NCC) of both volumes is used as a cost function. In this paper, the reference image is generated using the prior image constrained compressed sensing (PICCS) algorithm combined with the improved total variation (iTV). First preliminary experiments on clinical porcine data sets show promising results. CMHPR reduces streak artifacts and simultaneously preserves sharp edges without producing the artificial comic-like appearance of the PICCS + iTV reference volume.

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In this paper, we present an iterative motion estimation and compensation algorithm that uses projection data acquired during one single C-arm sweep. It uses the ECG information to parametrize a 4-D motion field that maps the sum of all ECG-gated volumes into a single reference volume at every iteration step in order to suppress apparent noise.

Additionally, a bilateral filter is applied to the reconstructed volume at every iteration step in order to suppress apparent noise.

B. ECG-gated FBP Volume Reconstruction

A certain number \( H \) of ECG-gated volumes \( f_h(x) \), with \( h = 1, \ldots, H \) at specific heart phases are reconstructed with an FDK reconstruction algorithm. The ECG-gating is performed by inserting a weighting function \( \lambda \) into the standard FDK approach. Let \( q_h \in [0,1] \) be the relative heart phase at which the reconstruction shall be carried out. The ECG-gated FDK reconstruction \( f_h(x) : \mathbb{R}^3 \rightarrow \mathbb{R} \) at voxel \( x \in \mathbb{R}^3 \) is given by

\[
f_h(x) = \sum_{i=1}^{N} \lambda(i, q_h) \cdot w(i, x) \cdot p_F(i, A(i, x)), \]

where \( N \) is the number of projection images, \( w : \mathbb{N} \times \mathbb{R}^3 \rightarrow \mathbb{R} \) is the FDK distance weight and \( p_F(i, u) : \mathbb{N} \times \mathbb{R}^2 \rightarrow \mathbb{R} \) is the filtered and redundancy-weighted projection data of the \( i \)-th image at pixel position \( u \). The pixel position is determined by the perspective projection of voxel \( x \), \( A : \mathbb{N} \times \mathbb{R}^3 \rightarrow \mathbb{R}^2, (i, x) \rightarrow A(i, x) = u \). The perspective projection \( A \) can be computed via pre-calibrated projection matrices. The weighting function \( \lambda \) can be a cosine- or rectangular-window [17]. Here, we use a strict rectangular gating function of minimal width, i.e. only one view per heart cycle is considered.

C. Final Volume Reconstruction

The final volume is defined as a sum volume \( f(x, s) \) consisting of the deformed ECG volumes \( f_h(x + s_{h,x}) \) with motion vector \( s_{h,x} \) at heart phase \( h \) and location \( x \):

\[
f(x, s) = \sum_{h=1}^{H} f_h(x + s_{h,x}). \]

The function \( f_h \) returns the ECG-gated, interpolated reconstructed object value at voxel \( x \) based on the motion vector \( s_{h,x} \) for the heart phase \( h \). In this paper, the motion compensated reconstruction and its derivative are based on a densely sampled motion vector field. That means for each voxel \( x \in \Omega \) at the \( h \)-th heart phase an individual displacement vector \( s_{h,x} \in \mathbb{R}^3 \) is given. \( \Omega \) denotes the area where cardiac motion is assumed.

D. Objective Function

The 4-D motion vector field is derived by optimizing an objective function \( L_{NCC}(s) \) so that the negative normalized cross correlation (NCC) between the sum volume \( f(x, s) \) and the reference volume \( f_s(x) \) is minimized. The metric ranges between \([-1,1]\). In order to define a dissimilarity measure, the negative correlation is considered here. Therefore, a value of -1 indicates a perfect positive linear relationship, a value of +1 a perfect negative linear relationship and values close to zero show no linear correlation between the volumes. The definition of the negative NCC [18], [19] combined with the algorithms were published [8]. A variety of algorithms minimizes an objective function related to the total variation (TV) [9]. In one approach called prior image constrained compressed sensing (PICCS), a-priori information of the same object is incorporated into the reconstruction [10], [11]. The PICCS algorithm was recently applied to interventional images using angiographic data from a C-arm system [12], [13]. In general, volumes reconstructed with TV regularization have an artificial look and are highly smoothed compared to a standard FDK reconstruction. They are piecewise constant in homogenous regions and can lose small structures [14].

The presented motion estimation and compensation scheme is built up from different components: First, a reference volume needs to be generated. Second, the ECG-gated volumes representing different heart phases are reconstructed with a standard FBP algorithm. The final volume is defined by the sum over the deformed ECG-gated volumes. The deformation depends on the 4-D motion vector field (MVF). The MVF is built up from different components: First, a reference volume needs to be generated. Second, the ECG-gated volumes consisting of the deformed ECG volumes \( f_{h,x}(x) \) with motion vector \( s_{h,x} \) at heart phase \( h \) and location \( x \):

\[
f(x, s) = \sum_{h=1}^{H} f_h(x + s_{h,x}). \]
The computational formula for the variance [20] is given by

\[ \mathcal{L}_{\text{NCC}}(s) = -\frac{n_{rf}(s)}{\sqrt{n_{rr} \cdot n_{ff}(s)}}, \]  

where

\[ n_r = \sum_{x \in \Omega} f_r(x) \]  

\[ n_f(s) = \sum_{x \in \Omega} f(x, s) \]  

\[ n_{rr} = \sum_{x \in \Omega} f_r(x)^2 - \frac{1}{|\Omega|} n_r^2 \]  

\[ n_{ff}(s) = \sum_{x \in \Omega} f(x, s)^2 - \frac{1}{|\Omega|} n_f(s)^2 \]  

\[ n_{rf}(s) = \sum_{x \in \Omega} f_r(x) f(x, s) - \frac{1}{|\Omega|} n_r \cdot n_f(s). \]  

### E. Optimization Strategy

The objective function is minimized by a gradient-based quasi-Newton method, a limited-memory Broyden-Fletcher-Goldfarb-Shanno optimizer (L-BFGS) [21]. Usually, the quasi-Newton based methods converge in fewer iterations than gradient descent optimizers, but have a higher cost per iteration evaluation. For the optimization, the derivative of the objective function with respect to the motion vector at every heart phase and voxel is required. It can be computed as

\[ \frac{\partial \mathcal{L}_{\text{NCC}}(s)}{\partial s_{h,x}} = -\left( \frac{1}{\sqrt{n_{rr} \cdot n_{ff}(s)}} \right) \frac{\partial n_{rf}(s)}{\partial s_{h,x}} - \frac{n_{rf}(s)}{2 \sqrt{(n_{rr} \cdot n_{ff}(s))^3}} \frac{\partial n_{ff}(s)}{\partial s_{h,x}} \]  

where the remaining components are given by

\[ \frac{\partial n_{rf}(s)}{\partial s_{h,x}} = \left( f_r(x) - \frac{n_r}{|\Omega|} \right) \frac{\partial f(x, s)}{\partial s_{h,x}} \]  

and

\[ \frac{\partial n_{ff}(s)}{\partial s_{h,x}} = 2 \left( f(x, s) - \frac{n_f(s)}{|\Omega|} \right) \frac{\partial f(x, s)}{\partial s_{h,x}}. \]  

Finally, putting all components together we arrive at the derivative of the objective function:

\[ \frac{\partial \mathcal{L}_{\text{NCC}}(s)}{\partial s_{h,x}} = -\kappa(x, s) \cdot \frac{\partial f(x, s)}{\partial s_{h,x}}, \]  

where

\[ \kappa(x, s) = \left( f_r(x) - \frac{n_r}{|\Omega|} \right) \left( f(x, s) - \frac{n_f(s)}{|\Omega|} \right). \]  

Only \( \kappa(x, s) \) depends on the objective function and can be easily adapted if a different objective function is used. In order to guarantee a smooth motion vector field, a spatial and temporal Deriche filter is applied to the 4-D motion vector gradient. Additionally, a spatial Deriche filter is also applied to the gradient weighting term \( \kappa(x, s) \) [22, 23].

### F. Implementation Details

Due to memory limitations when using a quasi-Newton optimizer and to reduce computation time, the motion vector field was first computed on downsampled volumes at a resolution of 128×128×128 voxels and upsampled onto the final reconstructed volume size by cubic spline interpolation. The initial motion vector field was set to zero in all dimensions. The weighting parameter \( \alpha \) for the PICCS algorithm was set to 0.5. The relaxation parameter \( \beta \) for the iTV optimization was set to 0.8 and the iTV parameter \( \omega \) to 0.8. For the bilateral filter,
the closeness parameter $\sigma_d$ was set to 0.25 and the similarity parameter $\sigma_r$ was set to 0.0001. The used filter mask has a radius of 2 voxels. The Deriche filter parameter $\alpha_d$ for spatial filtering was heuristically set to 0.94 and for temporal filtering to 2.12, i.e. a stronger smoothing in spatial than in temporal direction. The LBFGS optimizer of the VNL numerics library delivered with The Insight Segmentation and Registration Toolkit (ITK)\(^1\) was used for the optimization. The optimization procedure was performed until the termination criterion was reached. Here, the number of function evaluations was used which was set to 200. The number of iterations is implicitly given by the number of function evaluations. During the linesearch of the gradient update, the objective function is evaluated more than once if we are close to a minimum, hence less iterations are performed. In order to restrict the motion vector field to a local area where the heart motion is expected, a local motion mask enforces zero motion outside the defined local area. In this first approach the mask volume defining $\Omega$ is generated manually by the user. For a later version it is planned to use an automatic heart isolation software [24, [25].

III. EXPERIMENTAL SETUP

The method was applied to in-vivo data sets of two porcine models ($p_1, p_2$). Image acquisition was performed using an Artis Zee C-arm system (Siemens AG, Healthcare Sector, Forchheim, Germany). The acquisition time was 14.535 s capturing 381 projection images with 30 f/s, and an angular increment of 0.52° during one C-arm sweep. The isotropic pixel resolution was 0.31 mm/pixel (0.19 mm in isocenter) and the detector size 1240 × 960 pixel. The distance from source to detector was 1200 mm and from isocenter to source 750 mm. The heart rate was synchronized with the frame-rate of the imaging acquisition through external heart pacing. The considered heart phases are equal to the number of image frames per heart cycle. For porcine model $p_1$ a number of 32 heart cycles and $H = 12$ heart phases were imaged with an external pacing of $\approx 131$ bpm. For porcine model $p_2$ a number of 25 heart cycles and $H = 15$ heart phases were imaged with an external pacing of $\approx 105$ bpm. A volume of $\sim 150$ ml contrast fluid was administered intravenously at a speed of $p_1 = 10$ ml/s, $p_2 = 6.5$ ml/s , with a delay of 5 s and 8 s before the X-ray rotation was started. Image reconstruction was performed on an image volume of (25.6 cm)\(^3\) distributed on a 256\(^3\) voxel grid.

IV. RESULTS AND DISCUSSION

A. Visual Inspection

The reconstruction results of the 1st porcine model $p_1$ at a relative heart phase of 80% are shown in Figure 2. The standard FDK reconstruction averages over all heart phases which is visible at the doubling of the catheter and the blurred endocardium edges (Fig.2a). The ECG-gated reconstruction illustrates the sharp contours of the endocardium, however prominent streak artifacts are apparent (Fig.2b). Streak artifacts are reduced by the PICCS and iTV reconstruction (Fig.2c). However, the image still exhibits blurred streak artifacts and is smoothed. The presented CMHPR algorithm (Fig.2d). yields the best result. Streak artifacts are further reduced while keeping the spatial resolution. The same effects are visible in Figure 3 for a different relative heart phase of 30 % of the same porcine model $p_1$ and for the second porcine model $p_2$ for relative heart phases of 50% in Figure 4 and of 30 % in Figure 5.

B. Normalized Edge Response Profile

In order to quantify the results, the normalized edge response function (similar to the edge response in Prümmer et al. [7]) of all volumes is illustrated in Figure 6. The normalized edge response profile is computed as mean edge profile of the lines indicated in Figures 2, 3, 4 and 5 and normalized to [0,1]. The measurements were performed for the porcine model $p_1$ and a relative heart phase of 80% (Fig.6a) and 30% (Fig.6b). Similar measurements were performed for the second porcine model $p_2$ and a relative heart phase of 50% (Fig.6c) and 30% (Fig.6d). It can be seen that the FDK reconstruction loses the edge at the endocardium border. The sharp edge is reconstructed by the ECG-gating, however, it is affected by noise and streak artifacts. The CMHPR method preserves the sharp edge similar to the reference volume.

V. CONCLUSION

We have presented a new motion estimation and compensation algorithm by the combined multiple heart phase registration (CMHPR) which increases image quality for cardiac angiographic C-arm data. The presented algorithm was tested on two porcine models and first results are promising. The technique reduces streak artifacts and simultaneously preserves sharp edges without getting an artificial comic-like appearance.

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DISCLAIMER

The concepts and information presented in this paper are based on research and are not commercially available.

REFERENCES


\(^1\) www.itk.org
Figure 2: Experimental results in porcine model $p_1$ of the central slice and a relative heart phase of $\approx 80\%$ (W 1630 HU, C 50 HU, slice thickness 1.0 mm). The ECG-gated reconstruction was windowed to be visually comparable.

Figure 3: Experimental results in porcine model $p_1$ of the central slice and a relative heart phase of $\approx 30\%$ (W 1630 HU, C 50 HU, slice thickness 1.0 mm). The ECG-gated reconstruction was windowed to be visually comparable.

Figure 4: Experimental results in porcine model $p_2$ of the slice 108 and a relative heart phase of $\approx 50\%$ (W 1630 HU, C 50 HU, slice thickness 1.0 mm). The ECG-gated reconstruction was windowed to be visually comparable.

Figure 5: Experimental results in porcine model $p_2$ of the slice 108 and a relative heart phase of $\approx 30\%$ (W 1630 HU, C 50 HU, slice thickness 1.0 mm). The ECG-gated reconstruction was windowed to be visually comparable.
Figure 6: Normalized edge response profile of the four different reconstructions of two heart phases and the two porcine models $p_1$ and $p_2$. 

(a) Porcine model $p_1$ and heart phase 80%. Corresponding lines in Figure 2.

(b) Porcine model $p_1$ and heart phase 30%. Corresponding lines in Figure 3.

(c) Porcine model $p_2$ and heart phase 50%. Corresponding lines in Figure 4.

(d) Porcine model $p_2$ and heart phase 30%. Corresponding lines in Figure 5.