

# Pre-processing

## Filtering

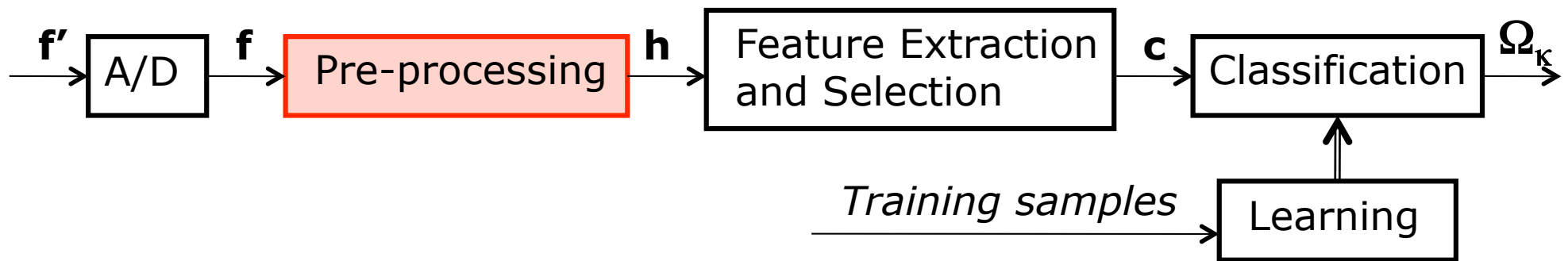


**Dr. Elli Angelopoulou**

**Lehrstuhl für Mustererkennung (Informatik 5)**

**Friedrich-Alexander-Universität Erlangen-Nürnberg**

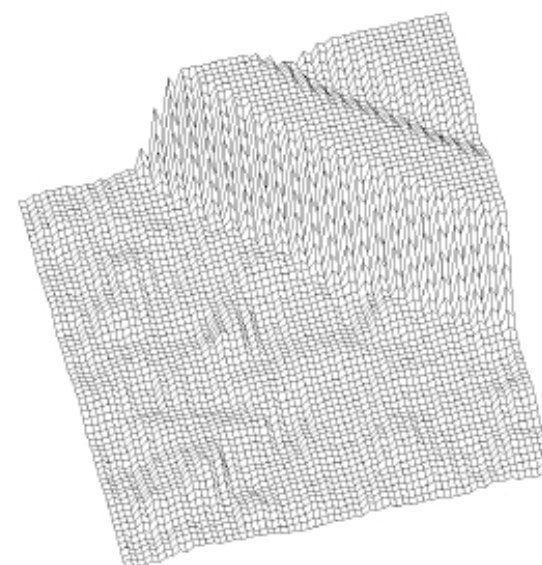
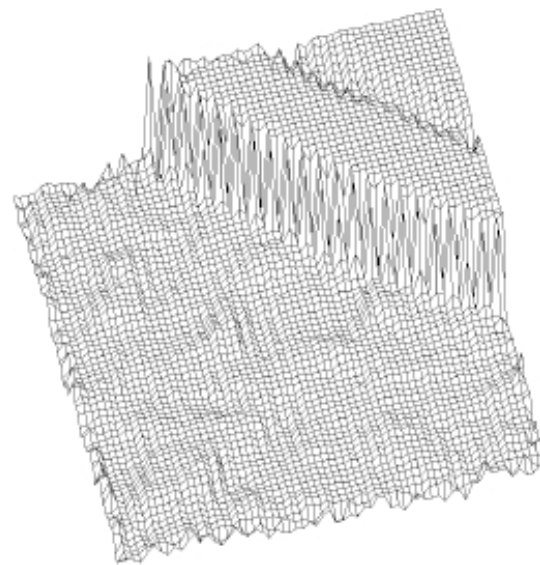
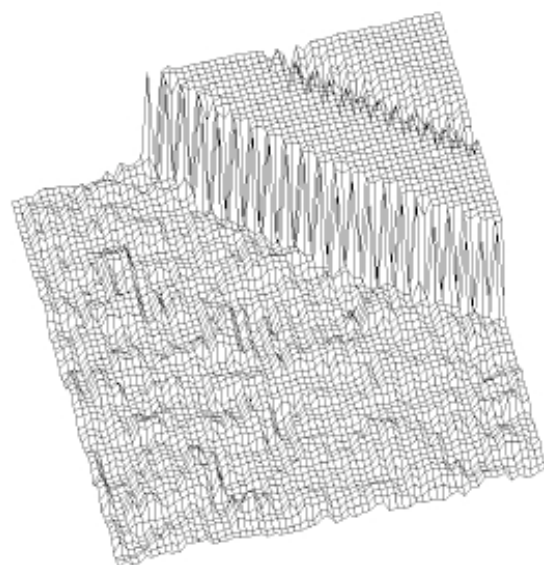
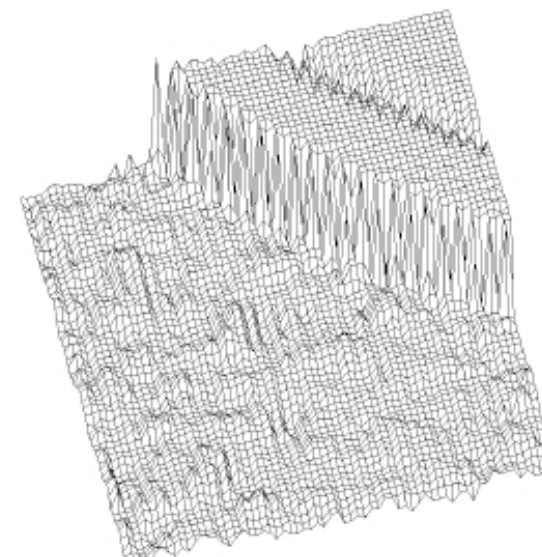
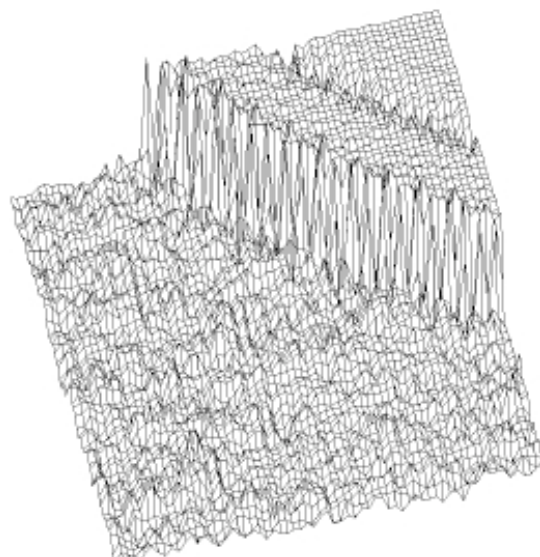
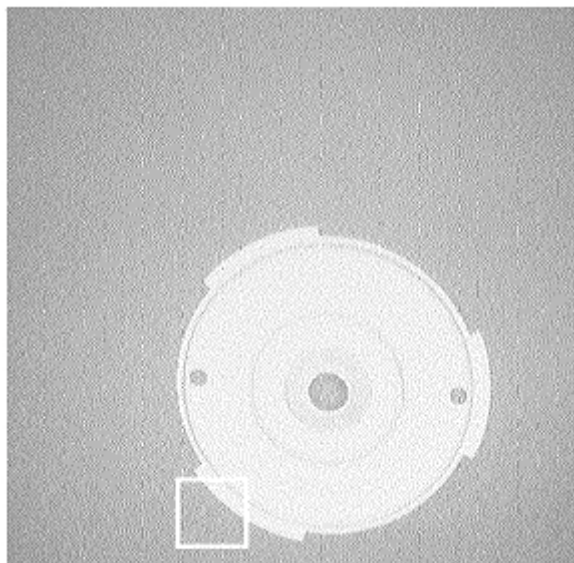
# Pattern Recognition Pipeline



- The goal of pre-processing is to transform a signal  $f$  to another signal  $h$  so that the resulting signal  $h$ 
  - makes subsequent processing easier
  - makes subsequent processing better (more accurate)
  - makes subsequent processing faster
- Already studied *histogram equalization* and *thresholding*.



# Pre-processing Example



# Noise Sources



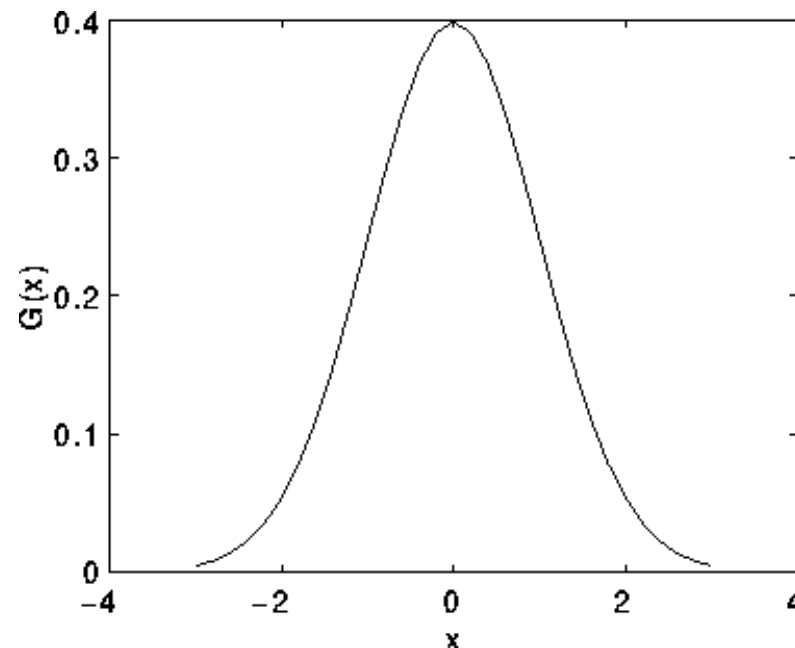
- Photon noise: variation in the #photons falling on a pixel per time interval  $T$ .
- Saturation: each pixel can only generate a limited amount of charge.
- Blooming: saturated pixel can overflow to neighboring pixels.
- Thermal noise: heat can free electrons and generate a response when there is none.
- Electronic noise.
- Burned pixels.
- Black is not black.
- Keep in mind: Camera response may not be linear over the number of photons falling on a surface (camera gamma)



# Detector Noise



- Source of noise: the discrete nature of radiation, i.e. the fact that each imaging system is recording an image by counting photons.
- Can be modeled as an independent additive noise which can be described by a zero-mean Gaussian.



# Salt and Pepper Noise



- A common form of noise is caused by *data drop-out noise*.
- It is also known as commonly referred to as intensity spikes, speckle or salt and pepper noise.
- Sources of error:
  - Errors in the data transmission.
  - Burned pixels: the corrupted pixels are either set to the maximum value (which looks like snow in the image) or are set to zero ("peppered" appearance), or a combination of the two.
  - Single bits are flipped over.
- Isolated/localized noise. It only affects individual pixels

# Filtering



- Most of the images we capture are noisy

- Goal:



- This notion of filtering is more general and can be used in a wide range of transformations that we may want to apply to images.



- Mathematically, a filter  $H$  can be treated as a function on an input image  $I$ :

$$H(I) = R$$

- Note: We use the terms *filter* and *transformation* interchangeably

# Linear Transformation



- A transformation  $H$  is **linear** if, for any inputs  $I_1(x,y)$  and  $I_2(x,y)$  (in our case input images), and for any constant scalar  $\alpha$  we have:

$$H(\alpha I_1(x,y)) = \alpha H(I_1(x,y))$$

and

$$H(I_1(x,y) + I_2(x,y)) = H(I_1(x,y)) + H(I_2(x,y))$$

- This means:
  - Multiplication in the input corresponds to multiplication in the output
  - Filtering an additive image is equivalent to filtering each image separately and then adding the results.



# Shift-Invariant Transformation



- A transformation  $H$  is **shift-invariant** if for every pair  $(x_0, y_0)$  and for every input image  $I(x, y)$ , such that

$$H(I(x, y)) = R(x, y)$$

we get

$$H(I(x - x_0, y - y_0)) = R(x - x_0, y - y_0)$$

- This means that the filter  $H$  does not change as we shift it in the image (as we move it from one position to the next).

# Convolution



- If a transformation (or filter) is linear shift-invariant (LSI) then one can apply it in a systematic manner over every pixel in the image.
- **Convolution** is the process through which we apply **linear shift-invariant filters** on an image.



- Convolution is defined as:

$$R(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} H(x - i, y - j) I(i, j)$$

and is denoted as:

$$R = H * I$$



## Another Look at Convolution

- Filtering often involves replacing the value of a pixel in the input image  $F$  with the weighted sum of its neighbors.
- Represent these weights as an image,  $H$
- $H$  is usually called the **kernel**
- The operation for computing this weighted sum is called **convolution**.

$$R = H * I$$

- Convolution is:

- commutative,  $H * I = I * H$
- associative,  $H_1 * (H_2 * I) = (H_1 * H_2) * I$
- distributive,  $(H_1 + H_2) * I = (H_1 * I) + (H_2 * I)$



# Smoothing via Simple Averaging

- One of the simplest filters is the mean filter:  $H = \begin{bmatrix} 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \\ 1/9 & 1/9 & 1/9 \end{bmatrix}$
- In this case,  $R(x, y) = \sum_{i=-1}^1 \sum_{j=-1}^1 I(x-i, y-j)H(i, j)$
- It is used for removing image noise, i.e. for smoothing.



Original image

\*  =

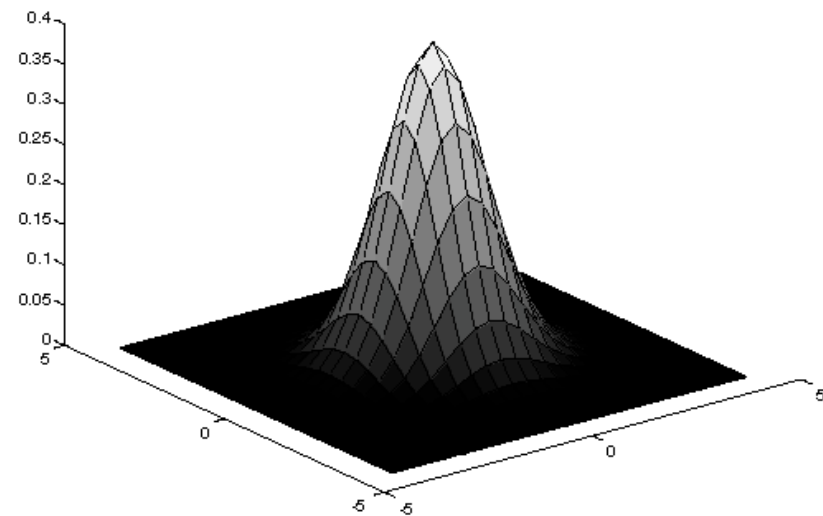


Image after mean filtering (25x25 kernel)

# Gaussian Smoothing



- Idea: Use a weighted average. Pixels closest to the central pixel are more heavily weighted.
- The Gaussian function has exactly that profile.
- Gaussian also better approximates the behavior of a defocused lens.



# Isotropic Gaussian Filter

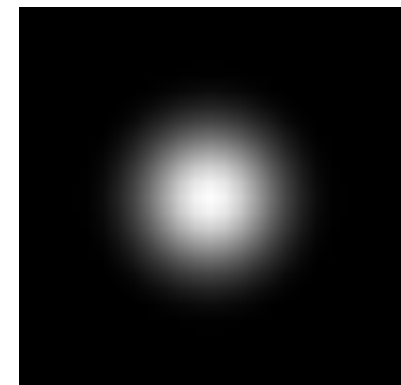


- To build a filter  $H$ , whose weights resemble the Gaussian distribution, assign the weight values on the matrix  $H$  according to the Gaussian function:

$$H(i, j) = e^{-(i^2 + j^2)/2\sigma^2}$$

$$H_{Gauss} = \begin{bmatrix} 1/16 & 1/8 & 1/16 \\ 1/8 & 1/4 & 1/8 \\ 1/16 & 1/8 & 1/16 \end{bmatrix}$$

- Small  $\sigma$ , almost no effect, weights at neighboring points are negligible.
- Large  $\sigma$ , blurring, neighbors have almost the same weight as the central pixel.
- Commonly used  $\sigma$  values: Let  $w$  be the size of the kernel  $H$ . Then  $\sigma = w/5$ .  
For example for a 3x3 kernel,  $\sigma = 3/5 = 0.6$




# Gaussian Smoothing Example



- Compared to mean filtering, Gaussian filtering exhibits no “ringing” effect.



Original image

\*  =

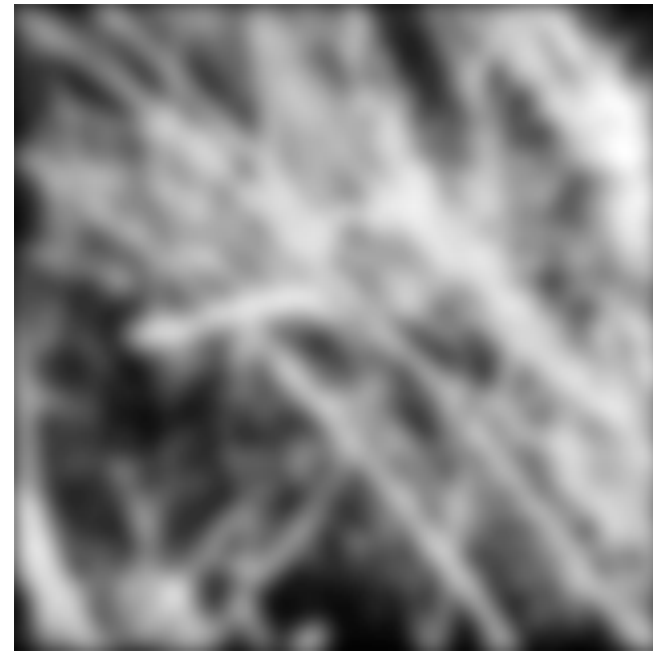


Image after Gaussian filtering (25x25 kernel)



# “Ringing” effect



Original image



Image after Mean filtering (25x25 kernel)

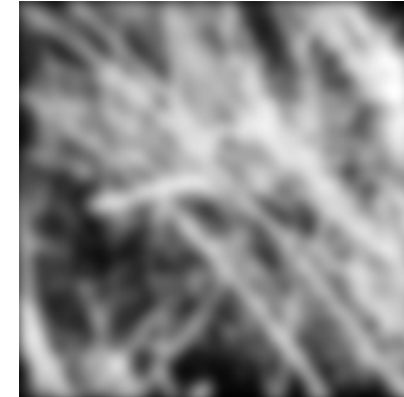
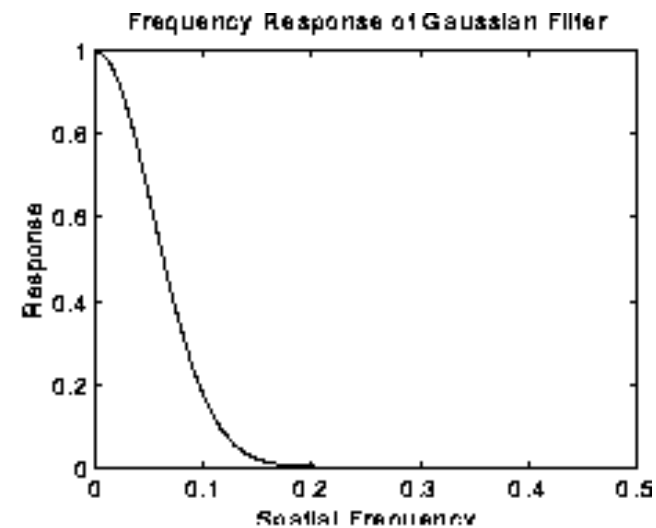
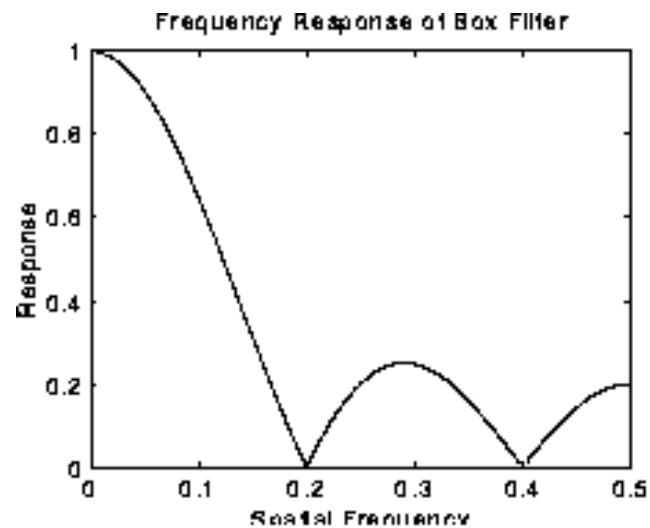


Image after Gaussian filtering (25x25 kernel)



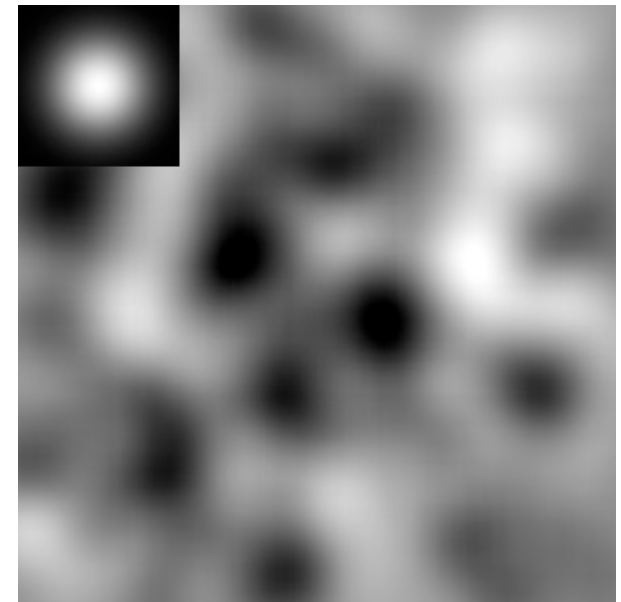
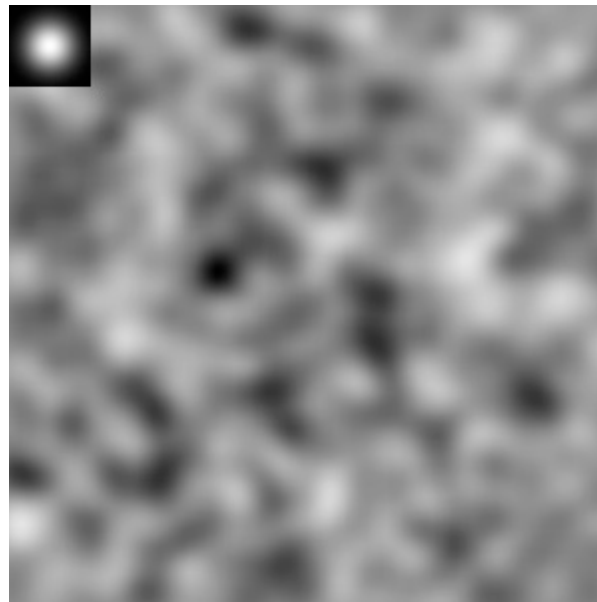
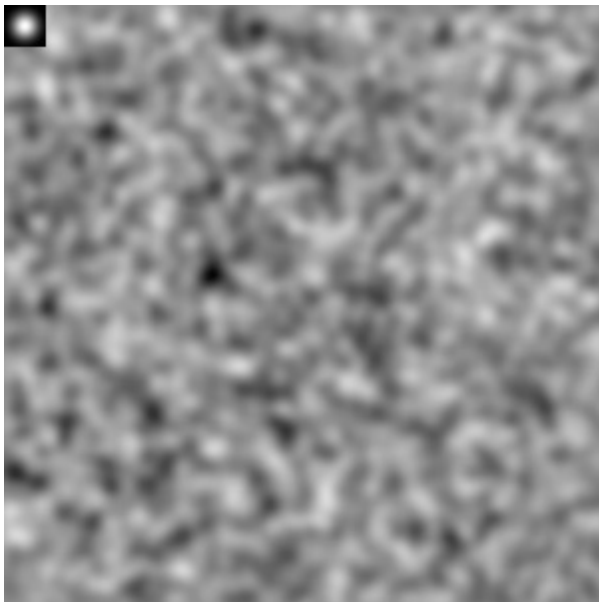
A close look at the frequency response of the two filters show that: compared to Gaussian filtering, mean filtering exhibits oscillations





## The Effect of $\sigma$

- Different  $\sigma$  values affect the amount of blurring, but also emphasize different characteristics of the image.



# Non-Linear Smoothing



- The **median** filter considers each pixel in the image in turn and looks at its nearby neighbors to decide whether or not it is representative of its surroundings.
- It replaces a pixel value with the median of all pixel values in the neighborhood.
- It is a relatively slow filter, because it involves sorting.
- Can **not** be implemented via convolution.



# Smoothing Examples



Original image



Image after 9x9 Mean filtering



Image after 9x9 Gaussian filtering

# Mean Filter



Original image



Image after 3x3  
Mean filtering



Image after 7x7  
Mean filtering



Image after applying  
3 times 3x3 Mean  
filtering

- Mean filtering is sensitive to outliers.
- It typically blurs edges.
- It often causes a ringing effect.

# Gaussian Filtering and Salt & Pepper Noise



Original image



Image with salt-pepper noise (1% prob. that a bit is flipped)



Image after 5x5 Gaussian filtering,  $\sigma=1.0$



Image after 9x9 Gaussian filtering,  $\sigma=2.0$

- Gaussian filtering works very well for images affected by Gaussian noise
- It is not very effective in removing Salt and Pepper noise.



# Median Filtering and Salt & Pepper Noise



Original image



Image with salt-pepper noise (5% prob. that a bit is flipped)



Image after 3x3 Median filtering



Image after 7x7 Median filtering



Image after applying 3 times 3x3 Median filtering

- Median filtering preserves high spatial frequency details.
- It works well when less than half of the pixels in the smoothing window have been affected by noise.
- It is not very effective in removing Gaussian noise.

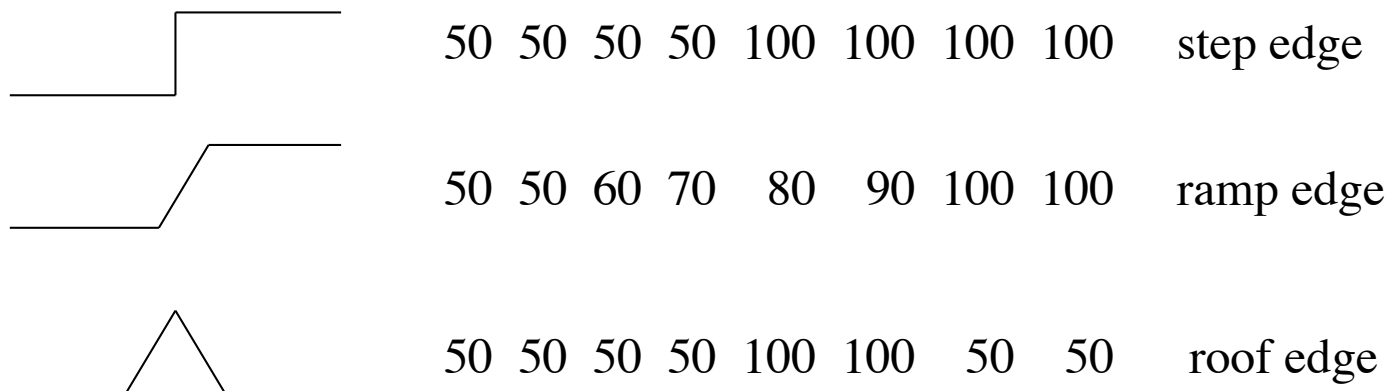
# Edges



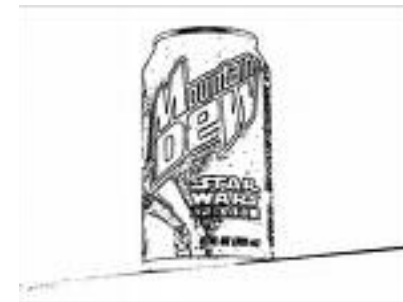
## ■ An edge is:

- A significant change in intensity values.
- Related to object boundaries, patterns (brick wall), shadows, etc.
- A property attached to each pixel.
- Calculated using the image intensities of neighboring pixels.

## ■ Examples of 1D Edges



# Edge Detection Example



Original images

Images after edge detection



# Edge Detection Steps



## 1. Noise Smoothing

- Suppress as much noise as possible without destroying edge information.

## 2. Edge Enhancement

- Design a filter that gives high responses at edges and low response at non-edge pixels.

## 3. Edge Localization

- Decide which high responses of the edge filter are responses to true edges and which ones are caused by noise or other artifacts.



# Types of Edge Detection

- Detecting edges is equivalent to detecting changes in intensity values.

- How do we detect change?

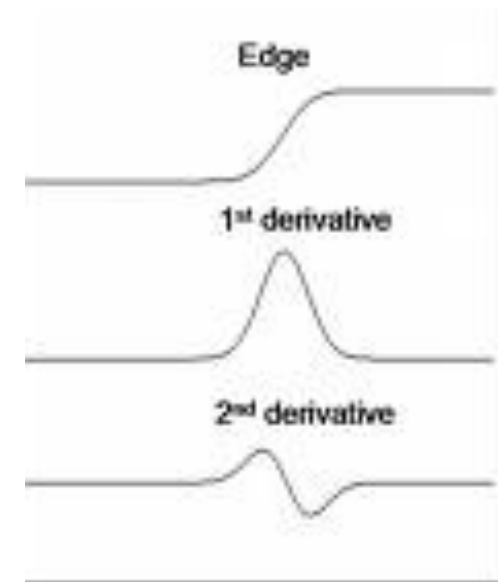
Differentiation

- Image is a 2D function

=> partial derivative in  $x$   
& partial derivative in  $y$

- If we take the 1<sup>st</sup> derivative we have **Gradient-based** edge detectors.

- If we take the 2<sup>nd</sup> derivative we have **Laplacian** edge detectors (look for zero-crossings).



# Gradient-Based Edge Detection



- The gradient vector  $\mathbf{G}(x,y)$ , at an image pixel  $I(x,y)$  is:

$$\mathbf{G}(x, y) = \left( \frac{\partial I(x, y)}{\partial x}, \frac{\partial I(x, y)}{\partial y} \right) = (I_x(x, y), I_y(x, y))$$

- The gradient vector points in the direction of maximum change.
- Its orientation (its angle with the x-axis) is given by:

$$\theta = \tan^{-1} \left( \frac{I_y(x, y)}{I_x(x, y)} \right)$$

- Its magnitude is given by:  $\|\mathbf{G}(x, y)\| = \sqrt{I_x^2(x, y) + I_y^2(x, y)}$

or its approximations:

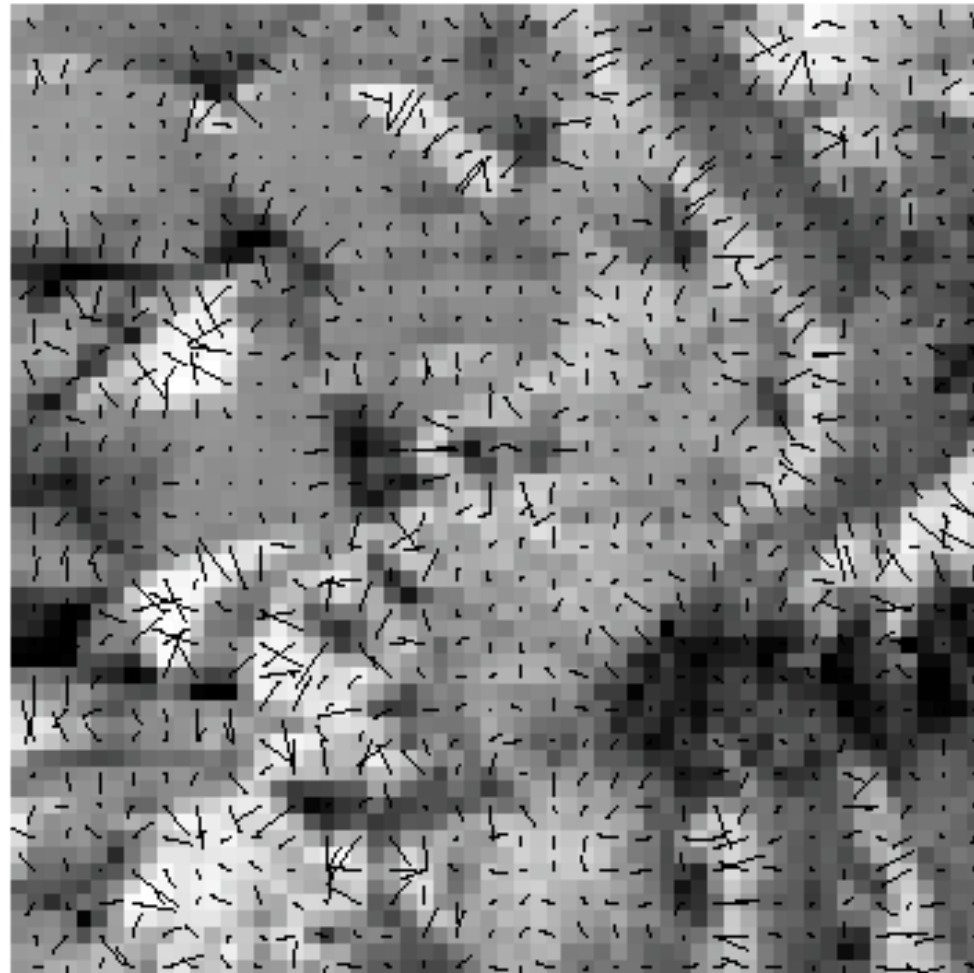
$$\|\mathbf{G}(x, y)\| \approx |I_x(x, y)| + |I_y(x, y)|$$

$$\|\mathbf{G}(x, y)\| \approx \max(|I_x(x, y)|, |I_y(x, y)|)$$

# Gradient Vector Image



- An image showing the gradient vectors themselves.
- The length of the gradient vector corresponds to its magnitude.



# Implementation



- By definition:

$$\partial I(x, y) / \partial x = \lim_{\varepsilon \rightarrow 0} \left( \frac{I(x, y) - I(x - \varepsilon, y)}{\varepsilon} \right)$$

- In the discrete world differentiation is approximated by finite differencing:

$$I_x(x, y) = \partial I(x, y) / \partial x \approx \frac{I[x, y] - I[x - \Delta x, y]}{\Delta x}$$

- But since our smallest step is  $\Delta x = 1$ :

$$I_x(x, y) = \partial I(x, y) / \partial x = I[x, y] - I[x - 1, y]$$
$$I_y(x, y) = \partial I(x, y) / \partial y = I[x, y] - I[x, y - 1]$$

## Implementation (continued)



- We can express this operation in a kernel form:

$$H_x = I_x = \begin{bmatrix} -1 & +1 \end{bmatrix} \quad H_y = I_y = \begin{bmatrix} -1 \\ +1 \end{bmatrix}$$

- To make it less susceptible to noise we use the values of two consecutive rows or columns.

$$H_x = I_x = \begin{bmatrix} -1 & +1 \\ -1 & +1 \end{bmatrix} \quad H_y = I_y = \begin{bmatrix} -1 & -1 \\ +1 & +1 \end{bmatrix}$$

- These kernels, however, evaluate an approximation of the derivative at half-pixel locations,  $I_x[x - 1/2, y]$  and  $I_y[x, y - 1/2]$

# Common Edge Masks



## ■ Prewitt edge detection masks

$$P_x = \begin{bmatrix} -1 & 0 & +1 \\ -1 & 0 & +1 \\ -1 & 0 & +1 \end{bmatrix}$$

$$P_y = \begin{bmatrix} -1 & -1 & -1 \\ 0 & 0 & 0 \\ +1 & +1 & +1 \end{bmatrix}$$

## ■ Sobel edge detection masks

$$S_x = \begin{bmatrix} -1 & 0 & +1 \\ -2 & 0 & +2 \\ -1 & 0 & +1 \end{bmatrix}$$

$$S_y = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ +1 & +2 & +1 \end{bmatrix}$$

# Gradient Edge Detection Process



- Given an input image  $I$ , the gradient-based edges are computed as follows:
  1. Compute  $I_x = H_x * I$
  2. Compute  $I_y = H_y * I$
  3. Compute  $\|\mathbf{G}(x, y)\|$  using your favorite method
  4. If  $\|\mathbf{G}(x, y)\| \geq t$   
then pixel  $(x, y)$  is an edge-pixel (*edge*)  
compute the angle  $\theta$  for that pixel.





# Gradient Edge Detector Example



Original image



Image after edge detection

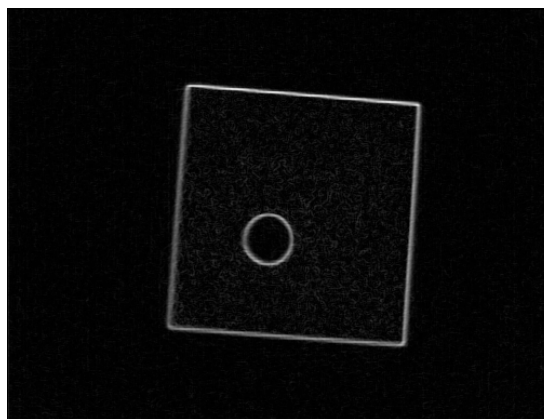
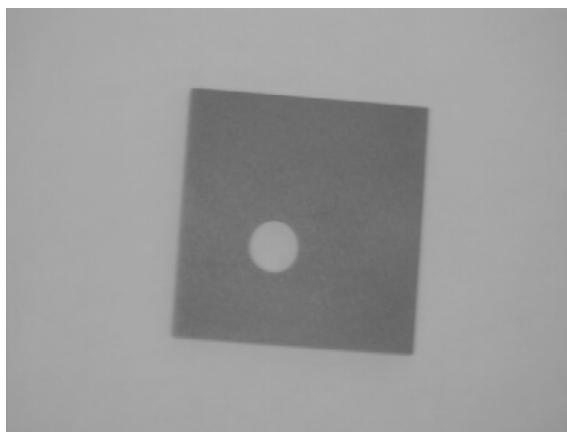
# Canny Edge Detector



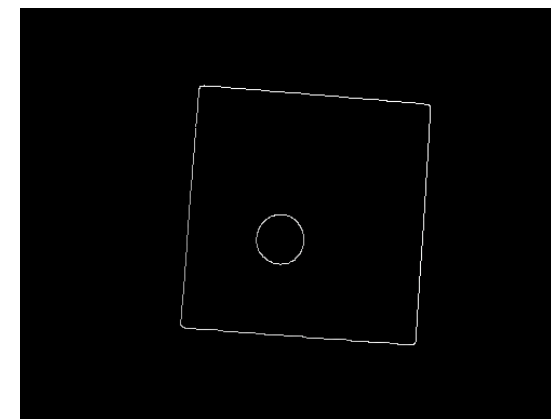
- After a gradient-based edge image is created, the Canny method uses optimization to systematically clean noise effects. It uses two separate optimization processes:
  1. Non-maximum suppression
    - A single real edge may appear as having wide ridges around it.
    - Non-maximum suppression thins such ridges down to 1-pixel wide edges.
  2. Hysteresis thresholding
    - Use a pair of threshold values. The high threshold is used as a first rough screening. For the edge pixels that survive this first screening, follow chains (contours) of edges. Use those edges on the chain which are above the second, lower, threshold.
- Canny proved that this is the optimal edge detection method.
- Due to the optimization post-processing, it is slower than the basic gradient-based edge detectors.



# Sobel versus Canny

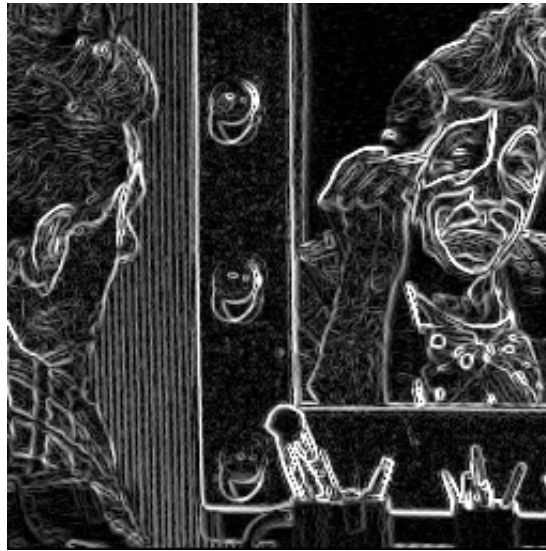


Sobel

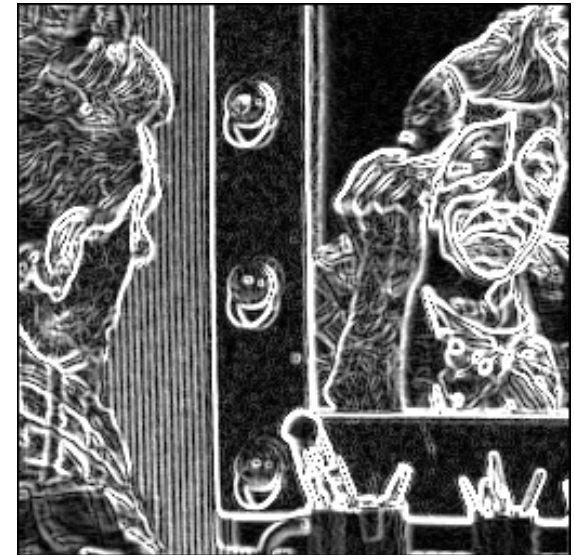


Canny

# Roberts vs. Sobel



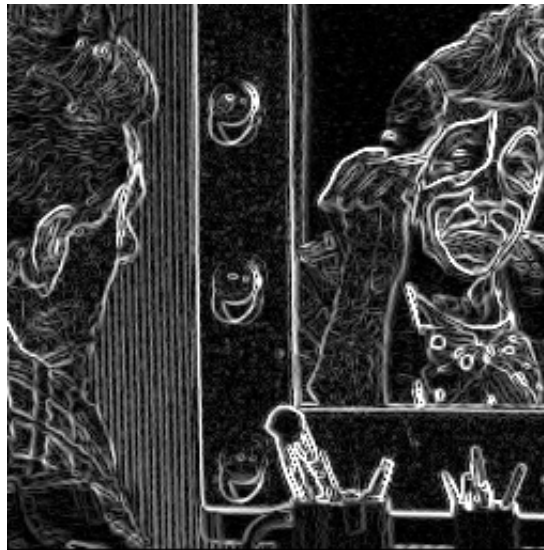
Roberts



Sobel



# Roberts vs. Canny



Roberts



Canny

$$\sigma = 1, t_l = 1, t_h = 255$$

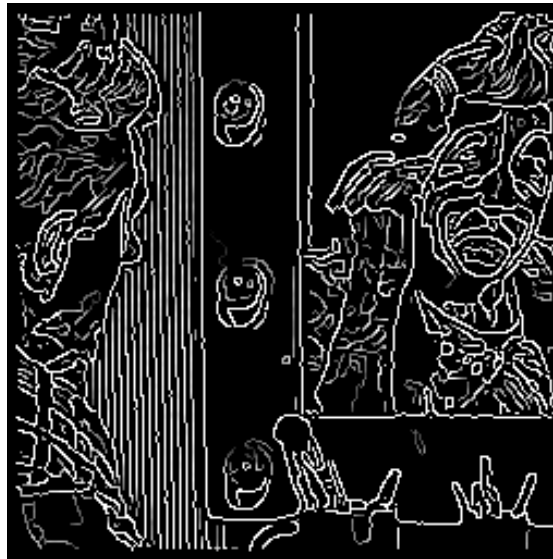


# Canny Edge Detector



Canny

$\sigma = 1, t_l=220, t_h= 255$



Canny

$\sigma = 1, t_l=1, t_h= 128$



Canny

$\sigma = 2, t_l=1, t_h= 128$



# LSI Filtering - Review



- We are focusing on linear shift-invariant (LSI) filters.



- Such filters are typically applied to an image through convolution:

$$R(x, y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} H(x - i, y - j) I(i, j)$$

- In practice, convolution can be seen as computing the weighted sum of a  $(2k+1) \times (2k+1)$  neighborhood centered around pixel  $(x, y)$ , where the filter  $H$  contains the applied weights.

$$R(x, y) = \sum_{i=-k}^k \sum_{j=-k}^k I(x - i, y - j) H(i, j)$$

# Convolution and LSI filtering - Review



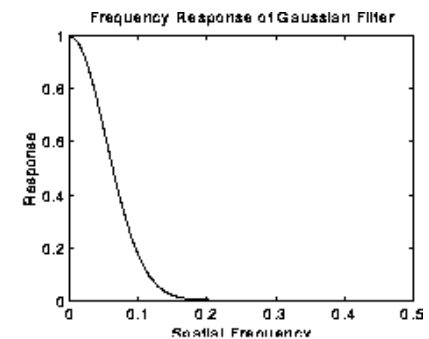
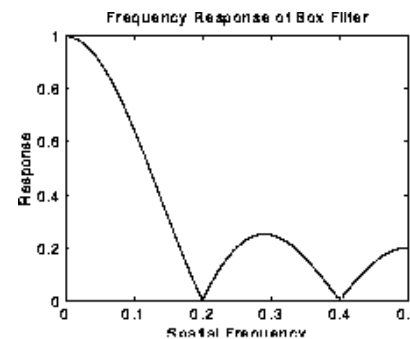
## ■ Important Properties of Convolution:

- commutativity,  $H * I = I * H$
- associativity,  $H_1 * (H_2 * I) = (H_1 * H_2) * I$
- distributivity,  $(H_1 + H_2) * I = (H_1 * I) + (H_2 * I)$

## ■ A very common application of filtering is for noise removal.

## ■ Two LSI smoothing filters are:

- Mean filter
- Gaussian filter



## ■ They are also known as low-pass filters, because in the frequency domain, they allow only transfer the low frequency information in the output image.



# Edge Detection - Review



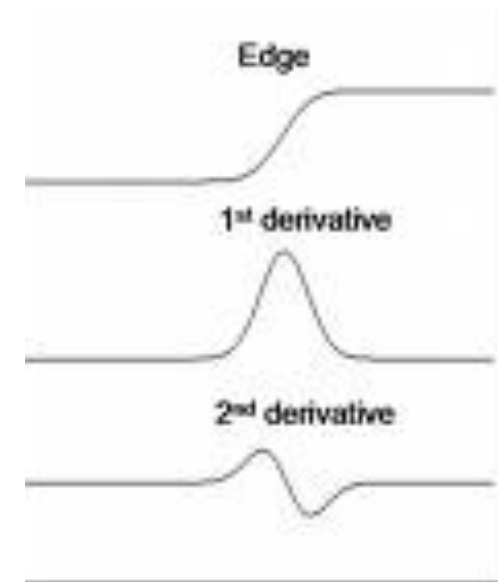
Original images

Images after edge detection



## Types of Edge Detection - Review

- Detecting edges is equivalent to detecting changes in intensity values.
- How do we detect change?  
Differentiation
- Image is a 2D function  
=> partial derivative in  $x$   
& partial derivative in  $y$
- If we take the 1<sup>st</sup> derivative we have **Gradient-based** edge detectors.
- If we take the 2<sup>nd</sup> derivative we have **Laplacian** edge detectors (look for zero-crossings).



# Gradient-Based Edge Detection - Review



- The gradient vector  $\mathbf{G}(x,y)$ , at an image pixel  $I(x,y)$  is:

$$\mathbf{G}(x, y) = \left( \frac{\partial I(x, y)}{\partial x}, \frac{\partial I(x, y)}{\partial y} \right) = (I_x(x, y), I_y(x, y))$$

- The gradient vector points in the direction of maximum change.
- Its orientation (its angle with the x-axis) is given by:

$$\theta = \tan^{-1} \left( \frac{I_y(x, y)}{I_x(x, y)} \right)$$

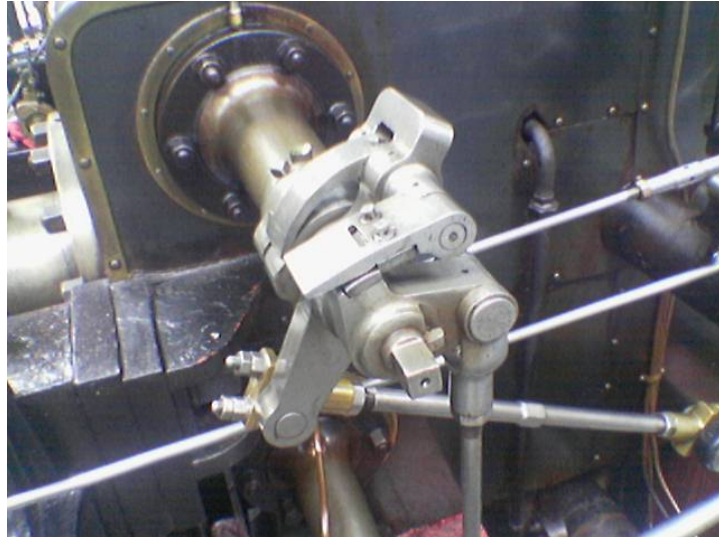
- Its magnitude is given by:  $\|\mathbf{G}(x, y)\| = \sqrt{I_x^2(x, y) + I_y^2(x, y)}$

or its approximations:

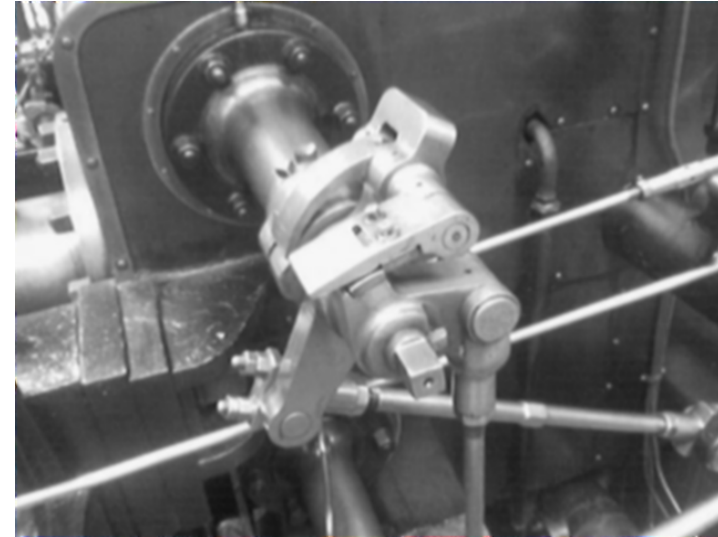
$$\|\mathbf{G}(x, y)\| \approx |I_x(x, y)| + |I_y(x, y)|$$

$$\|\mathbf{G}(x, y)\| \approx \max(|I_x(x, y)|, |I_y(x, y)|)$$

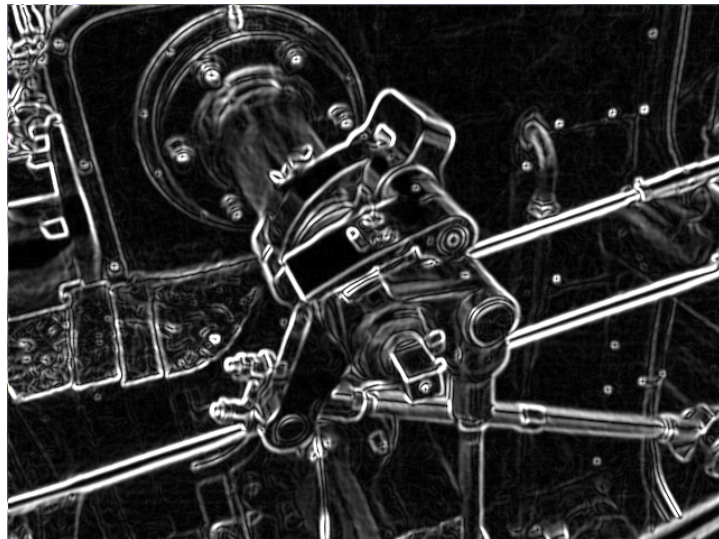
# Gradient-Based Edge Detector Example



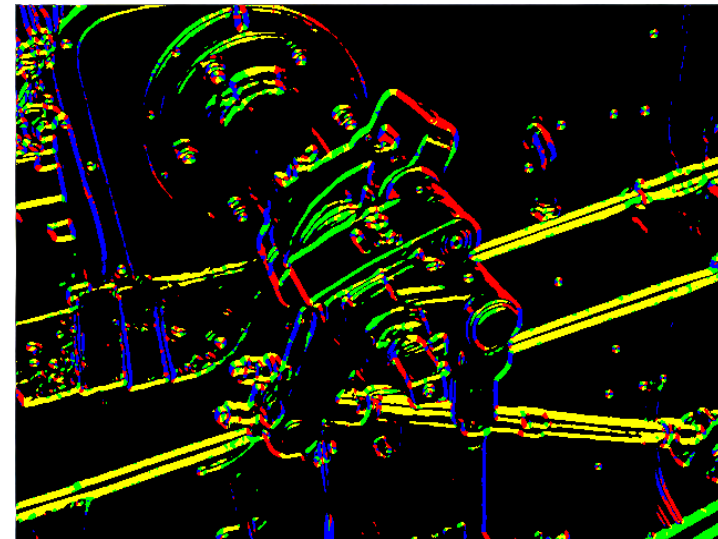
Original image



Step 1: Conversion to grayscale and smoothing with 5x5 Gaussian



Step 2: Sobel edge detector – edge magnitude image



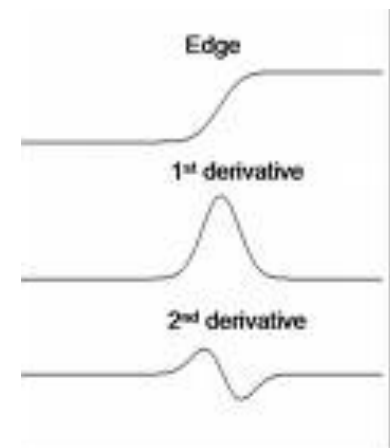
Step 2: Sobel edge detector – edge orientation image

# Second Order Derivative



- Another way to detect an extremal first derivative is to look for a zero-valued 2<sup>nd</sup> derivative.
- A popular calculus tool that gives the magnitude of change in a bivariate function without direction information is the Laplacian.

$$\nabla^2(I(x, y)) = \left( \frac{\partial^2 I(x, y)}{\partial x^2} + \frac{\partial^2 I(x, y)}{\partial y^2} \right)$$



- Note that the result of the Laplacian is a scalar.

# Laplacian Implementation



- Again differentiation is approximated by finite differencing.

$$\begin{aligned}\partial I^2(x, y) / \partial x^2 &= \partial(I_x(x, y)) / \partial x \\ &= \partial(I[x, y] - I[x - 1, y]) / \partial x \\ &= \partial(I[x, y]) / \partial x - \partial(I[x - 1, y]) / \partial x \\ &= (I[x + 1, y] - I[x, y]) - (I[x, y] - I[x - 1, y]) \\ &= I[x + 1, y] - 2I[x, y] + I[x - 1, y]\end{aligned}$$

- Written as a mask, we get:  $H_x = {}^2I_x = \begin{bmatrix} 0 & 0 & 0 \\ 1 & -2 & 1 \\ 0 & 0 & 0 \end{bmatrix}$

# Laplacian Implementation



- Similarly, for the 2<sup>nd</sup> partial derivative with respect to  $y$ , we get:

$$H_y = {}^2I_y = \begin{bmatrix} 0 & +1 & 0 \\ 0 & -2 & 0 \\ 0 & +1 & 0 \end{bmatrix}$$

- By adding the two together, we get the Laplacian mask:

$$H_{Lap} = {}^2I_x + {}^2I_y = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

- If we want to use all 8 neighbors, we can use:

$$H_{Lap} = \begin{bmatrix} 1 & 4 & 1 \\ 4 & -20 & 4 \\ 1 & 4 & 1 \end{bmatrix}$$

# Simple Laplacian Example



- When we convolve an image that contains a significant change in values (i.e. edge) with a Laplacian kernel, we get a new image with negative values on one side of the edge and positive values on the other side of the edge.

- For example:

Input image										Image after the Laplacian									
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0
2	2	2	2	2	2	8	8	8	8	0	0	0	0	0	6	-6	0	0	0

zero crossing





# Laplacian of Gaussian



- The computation of 2<sup>nd</sup> order derivatives is very sensitive to noise.
- Solution: Smooth first the image  $I$  with a Gaussian  $H_{Gauss}$  and then apply the Laplacian  $H_{Lap}$  on the image.

$$R_{LapEdge} = H_{Lap} * (H_{Gauss} * I)$$

- Convolution is associative.

$$R_{LapEdge} = (H_{Lap} * H_{Gauss}) * I$$

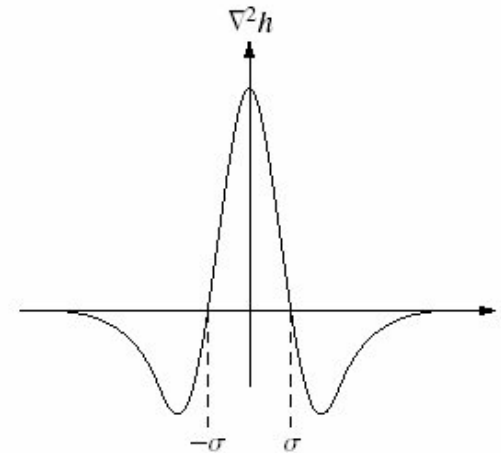
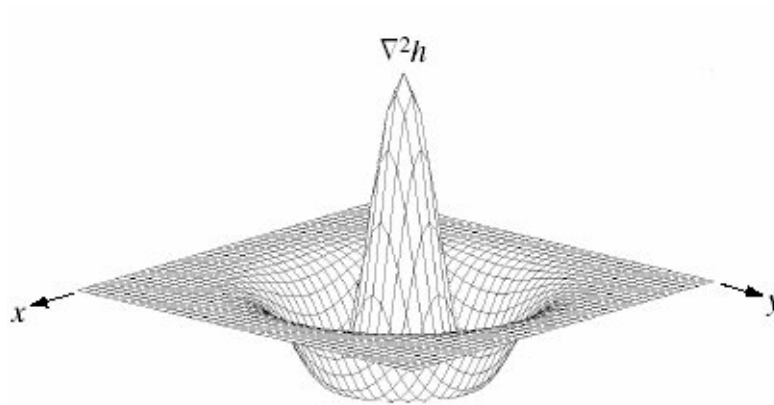
- The combined filter  $(H_{Lap} * H_{Gauss})$  is nothing more than computing the Laplacian of the Gaussian (LoG):

$$\begin{aligned} \nabla^2 (G_{Gauss}(x, y)) &= \nabla^2 (e^{-(x^2+y^2)/2\sigma^2}) \\ &= \frac{(x^2 + y^2 - \sigma^2)}{\sigma^4} (e^{-(x^2+y^2)/2\sigma^2}) \end{aligned}$$

# LoG Kernel



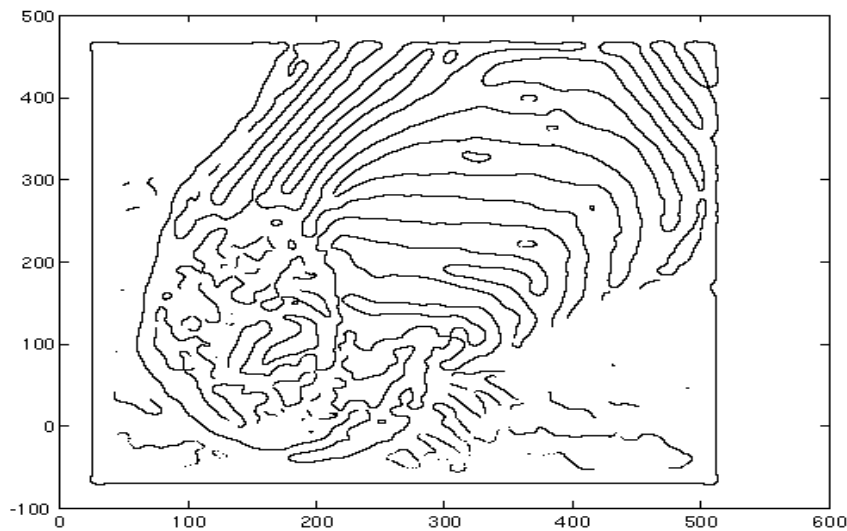
- The LoG function,  $\nabla^2(G_{gauss}(x, y))$  looks like a “mexican hat”.



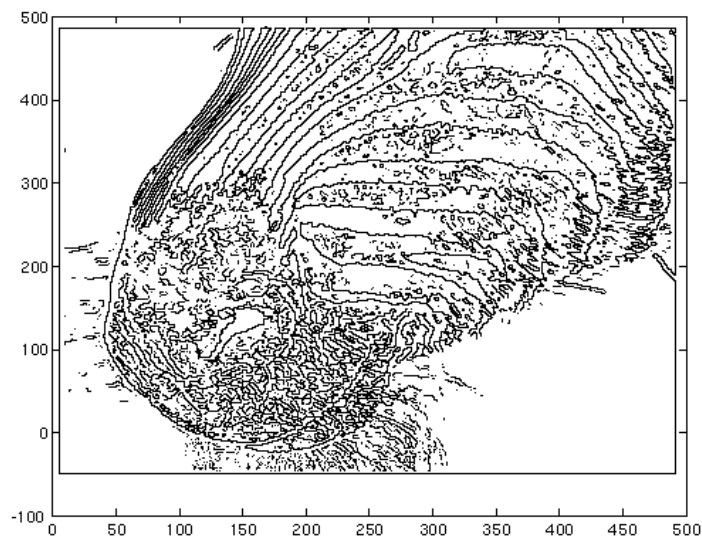
- $\nabla^2(G_{gauss}(x, y))$  can also be approximated by a convolution kernel:

$$H_{LoG} = \begin{bmatrix} 0 & 0 & -1 & 0 & 0 \\ 0 & -1 & -2 & -1 & 0 \\ -1 & -2 & 16 & -2 & -1 \\ 0 & -1 & -2 & -1 & 0 \\ 0 & 0 & -1 & 0 & 0 \end{bmatrix}$$

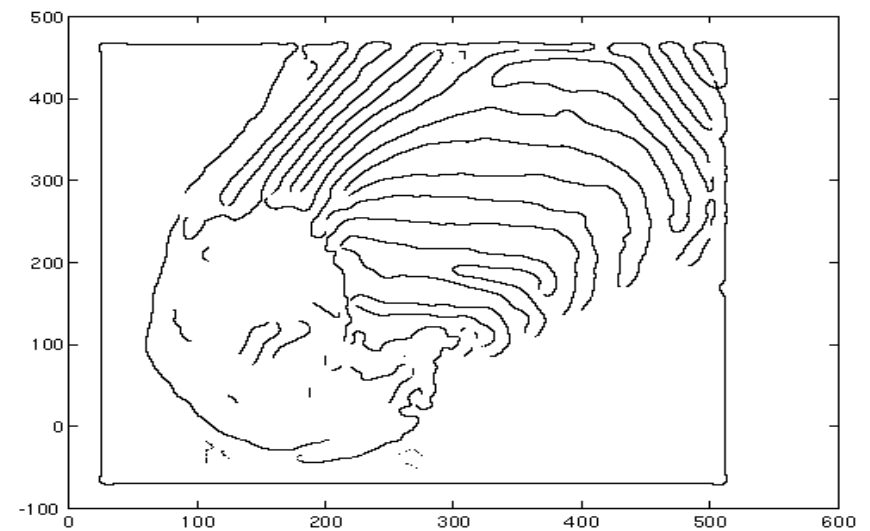
# Examples of LoG Zero Crossings



contrast=1

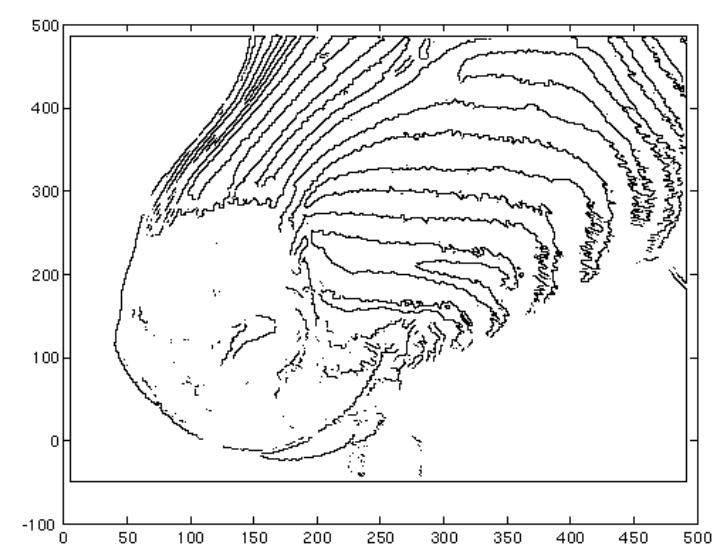


$\sigma = 4$



contrast=4

$\sigma = 2$



# Smoothing and Differentiation



- The concepts of first smoothing and then differentiating generalizes to all edge detection methods (both 1<sup>st</sup> and 2<sup>nd</sup> order derivative methods).
- Convolution is associative, so we can always create a combined filter and convolve (filter) the image only once.

$$R = H_{edge} * (H_{smooth} * I) = (H_{edge} * H_{smooth}) * I = H * I$$

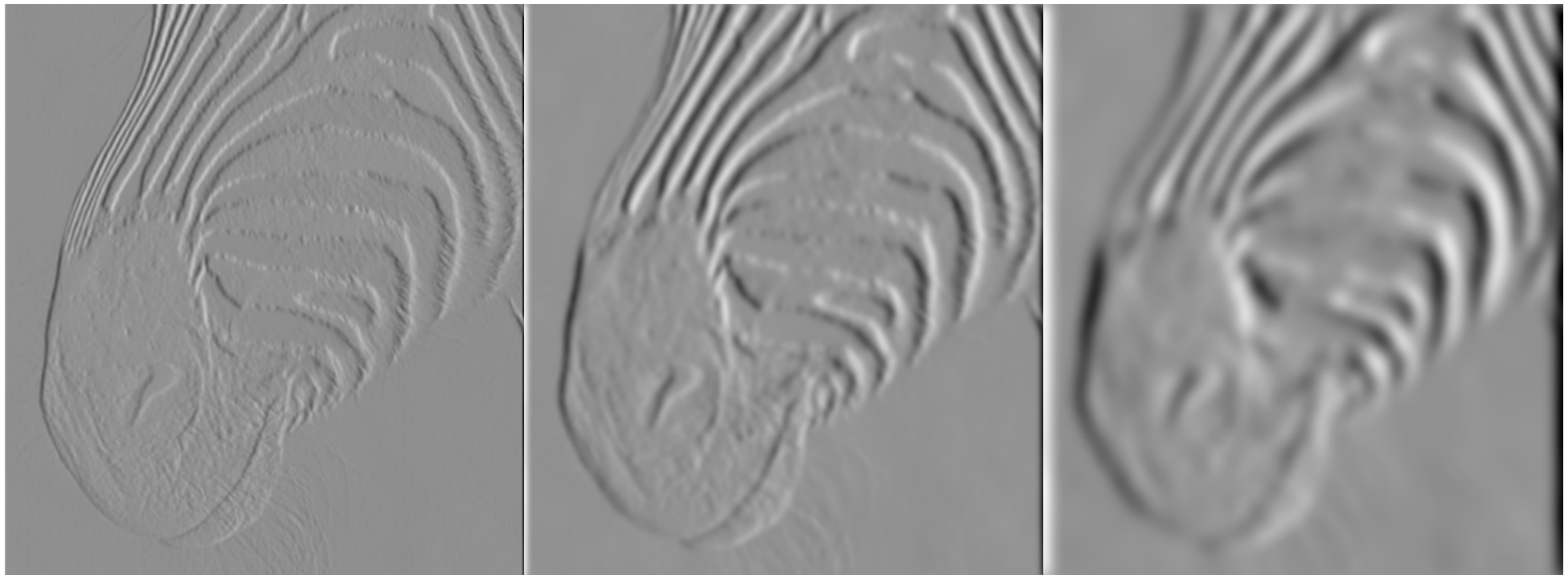
$$\text{where } H = H_{edge} * H_{smooth}$$

- By using different degrees of smoothing (Gaussian with different  $\sigma$  values or mean filters of different sizes, i.e. 3x3, 5x5, 7x7, etc.) we can obtain a hierarchy, a pyramid, of images with different levels of detail.

# Different Scales



- The scale of the smoothing filter affects the derivative estimates as well as the semantics of the recovered edges



No smoothing

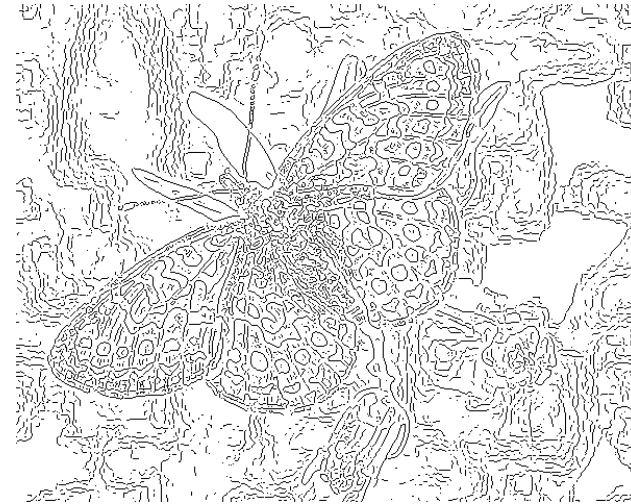
3x3 filter

7x7 filter

# Different Scales



Original image



Fine scale, high threshold



Coarse scale, low threshold



Coarse scale, high threshold

# Comments on Filtering



## ■ Design Decisions:

- Size of filter. There is no single good size. It depends on the size of the objects in the image.
- Speed versus accuracy: (Gaussian vs. Median, Gradient-based vs. Laplacian-based, Canny vs. Sobel)

## ■ Systematic approach: try different resolutions

- Either create a formal model for each resolution and study the change of the model at different resolutions.
- Or maintain a tree (pyramid) of images at different resolutions.

## ■ Multi-resolution example:

Apply an edge detector at different resolutions of Gaussians.

Perform numerical optimization to find the best response for the particular image.

Optimal for edges corrupted by white noise.





# Gaussian Pyramid Example





# Sharpening



- A very common filtering operation for contrast enhancement in images is *image sharpening*.
- The goal of image sharpening is to produce a more visually pleasing image:
  - Texture and finer details are made more prominent
  - The image looks sharper, crisper.



## Sharpening - continued



- Image sharpening almost always involves improving the parts of the image where a sudden change in intensity or color occur, since this is where inaccuracies are introduced by the digital data capturing process.
- What filtering operation do we know that gives a high response at sudden changes in intensity or color?
- Edge Detector,  $H_{edge}$
- A simple way to achieve sharpening is to superimpose the original image with the magnitude of the edge image.

$$R = I + c(I * H_{edge})$$

## UnSharp Mask



- Most image processing software packets perform sharpening using the UnSharp Mask (USM).
- It is based on an old photographic film technique.
- It is called unsharp masking, because it first blurs the image (unsharpens it)

$$R_1 = I * H_{smooth}$$

- An unsharp mask, UM, for the entire image is created by thresholding the absolute difference of the original and the blurred image.

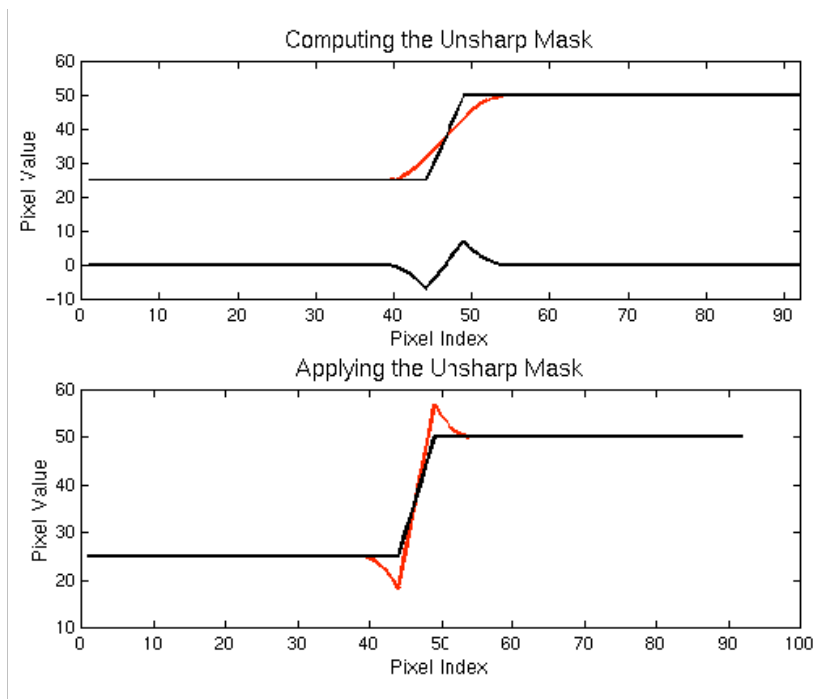
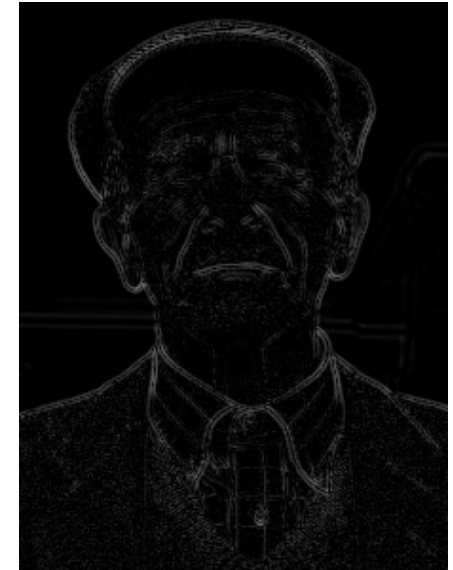
$$UM(x,y) = \begin{cases} 1 & \text{if } |I(x,y) - R_1(x,y)| > \theta \\ 0 & \text{otherwise} \end{cases}$$

# UnSharp Mask - continued



- The unsharp mask is then scaled (to achieve the desired visual effect) and added to the original image. The scaling factor  $c$  is often called *amount*.

$$R_2 = I + cUM$$





# Image Sources

1. "Image with salt & pepper noise", Marko Meza.
2. "Set of images of Roberts vs. Canny vs. Sobel", Hypermedia Image Processing Reference at the University of Edinburgh.
3. "LoG plots", Simon Yu Ming, <http://hi.baidu.com/simonyuee/blog/item/446a911bf43cc91c8618bf8f.html>
4. Many of the smoothing and edge detection images are from the slides by D.A. Forsyth, University of California at Urbana-Champaign.
5. The bird sharpening example was done using Adobe Photoshop Lightroom, <http://mansurovs.com/how-to-properly-sharpen-images-in-lightroom>.
6. The unsharp mask example is copyrighted by Sean T. McHugh, <http://www.cambridgeincolour.com/tutorials/unsharp-mask.htm>