## Binocular Stereo



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## Stereo Vision

- Goal: Infer information about the 3-D structure and distances of a scene from two or more images taken from different viewpoints.
- A stereo system must solve two subproblems:
- Correspondence problem
- Reconstruction
- Correspondence Problem: which point on the left image and on the right image are projections of the same scene point.
- Once the point correspondence is established, we can compute the relative shift, the disparity, between the two projections.
- Reconstruction: The disparity data is then converted to a 3D map. In order to transform the disparity data to 3D measurements, we need some form of knowledge about the geometry of the stereo system.


## Binocular Stereo Example



## Depth from Convergence



Human performance: up to 2-2.5 meters

## Depth from Binocular Disparity



P: converging point
C: object nearer projects to the outside of the P , disparity $=+$

F: object farther projects to the inside of the P , disparity $=-$

Sign and magnitude of disparity

## Simple Binocular Stereo Setup

- Parallel optic axes, i.e. the fixation point (the point where the 2 optic axes intersect) is at infinity.
- Both image planes lie on the same plane.
- Their scan lines are aligned (scan-line coherence), i.e. $y=y^{\prime}$.



## Correspondence and Triangulation

- When we correspond correctly (i.e. $\mathrm{q}_{\mathrm{L}}$ with $\mathrm{q}_{\mathrm{R}}$ and $\mathrm{p}_{\mathrm{L}}$ with $p_{R}$ ), the intersection of the corresponding rays gives the 3D location of scene point that generated the projections (i.e. Q and P accordingly).



## Impact of Correspondence

- A mistake in correspondence, e.g. $\mathrm{q}_{\mathrm{R}}$ is matched with $p_{L}$, will result in the intersection of rays that correspond to projection of distinct points ( Q and $P)$. As a result the wrong 3D location is recovered.



## Noise and Correspondence

- The noise in the image capture process (sensor noise, quantization, discretization) introduce inaccuracies in the projection rays that directly affect the triangulation process.



## Triangulation



- Assume that the correspondence has been correctly established.
- Under the simple binocular setup (parallel optic axes and scan-line coherence), the only difference between the two projections $\mathrm{q}_{\mathrm{L}}$ and $q_{R}$ is in the $x$-component, i.e. $x_{L}$ versus $x_{R}$.
- Let $T$ be the baseline, i.e. the distance between the two COPs.


## Triangulation



## Triangulation



From the similar triangles:

$$
\frac{x_{L}}{f}=\frac{X}{Z} \Rightarrow X=x_{L} \frac{Z}{f}
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## Triangulation



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From the $2^{\text {nd }}$ set of similar triangles:

$$
\frac{x_{R}}{f}=\frac{X-T}{Z}
$$

By replacing $X$ in the $2^{\text {nd }}$ eq.:

$$
\begin{aligned}
\frac{x_{R}}{f}= & \frac{x_{L} \frac{Z}{f}-T}{Z} \Rightarrow x_{R} Z=x_{L} Z-f T \\
& \Rightarrow Z=f \frac{T}{x_{L}-x_{R}}=f \frac{T}{d}
\end{aligned}
$$

where d is the disparity:

$$
d=x_{L}-x_{R}
$$

## Impact of Baseline



Large Baseline


Small Baseline

■What's the optimal baseline?

- Too small: large depth error
- Too large: difficult search problem
- Appearance may change between the 2 viewpoints
- Decrease in part of the scene that is mutually visible


## Vergence



Optical axes of the two cameras need not be parallel

■Solution: Vergence (turn cameras towards each other)

- Increases the field of view
- Increases accuracy in the correspondence


## Stereo Image Rectification

- So far we have assumed:
- parallel optic axes
- scan-line coherence
- This is usually not the case.
- Very often we have a verged camera setup, which means that the 2 optic axes are intersecting each other.
- Can we use the same math?



## Stereo Image Rectification

- Yes! Re-project the image planes onto a common plane parallel to the baseline (the line between optical centers).
- Two virtual image planes are created, which are now scanline coherent.
- Do all the computations on these rectified (virtual) image planes.



## Stereo Rectification Example

## Correspondence Problem

■ Assumptions:

- Most scene points are visible from both viewpoints
- Corresponding image regions look similar

■ It is a search problem: Given an element in the left image, search the right image to find the corresponding element.

■ Three underlying questions:

- What do we match between the two images? (objects, edges, pixels, sets of pixels?)
- What measure of similarity do we use?
- Can we search in a systematic way?


## Point Correspondence

Random dot stereograms


Julesz: had huge impact because it showed that recognition not needed for stereo.

## Point Correspondence in Practice



For each scan-line (more properly epipolar line)
For each pixel in the left image

- compare with every pixel on same epipolar line in right image
- pick pixel with minimum match cost
- This will never work, so:

Improvement: match windows

## Compare Regions around Points

- Idea: Compare intensity profiles around neighborhoods of potential points.
■ Elements to be matched are now image windows of fixed size.

■ The similarity measure is the correlation between windows in the two images.

## Similarity Metrics

$$
\begin{aligned}
& \text { f } \quad \mathbf{9} \\
& S S D=\sum_{[i, j] \in R}(f(i, j)-g(i, j))^{2} \\
& C_{f g}=\sum_{[i, j] \in R} f(i, j) g(i, j) \\
& \left.N C_{f g}=\frac{1}{n-1} \sum_{[i, j] \in R} \frac{(f(i, j)-\bar{f})(g(i, j)-\bar{g})}{\sigma_{f} \sigma_{g}}\right) \\
& \text { Most } \\
& \text { popular }
\end{aligned}
$$

For each window, match to the closest window on the horizontal (epipolar) line in the other image.

## Window Size



$\mathrm{W}=3$

$\mathrm{W}=20$

■ Smaller window: more detail, more noise.
■ Larger window: less noise, less detail
■ Better results with adaptive window size

## Compare Features

- Another Idea: Compute features and match only pixels based on their feature values.
- Possible features:
- Edges
- Lines...
- Pros: Possibly more unique values => easier correspondence
- Cons: Not all the pixels have a feature value => sparse correspondence; need for interpolation
- Often used in combination with hierarchical correspondence.


## Hierarchical Correspondence

- Allows faster computation
- Can handle large disparity ranges




## Stereo Example


H. Tao et al. "Global matching criterion and color segmentation based stereo"

## Reconstruction


H. Tao et al. "Global matching criterion and color segmentation based stereo"

## Image Sources

1. The slides on image rectification are courtesy of J. Chai, http://faculty.cs.tamu.edu/ichai/cpsc641 spring10/lectures/lecture9.ppt
2. A number of slides in this presentation have been adapted by the presentation of S. Narasimhan, http://ww.cs.cmu.edu/afs/cs/academic/class/15385-s06/lectures/ppts/lec-14.ppt
3. The Lincoln image is courtesy of S. Seitz.
4. The window-matching slide is courtesy of O. Camps.
5. The example slide on hierarchical correspondence algorithms is courtesy of ETH, http://www.inf.ethz.ch/personal/pomarc/courses/qcv/class07.ppt
