Pre-processing Filtering: Noise Suppression



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- The goal of pre-processing is to transform a signal f to another signal h so that the resulting signal h
 - makes subsequent processing easier
 - makes subsequent processing better (more accurate)
 - makes subsequent processing faster
- Already studied histogram equalization and thresholding.

Pre-processing Example







Noise Sources in Cameras



- Photon noise: variation in the #photons falling on a pixel per time interval T.
- Saturation: each pixel can only generate a limited amount of charge.
- Blooming: saturated pixel can overflow to neighboring pixels.
- Thermal noise: heat can free electrons and generate a response when there is none.
- Electronic noise.
- Burned pixels.
- Black is not black.





Keep in mind: Camera response may not be linear over the number of photons falling on a surface (camera gamma)

Detector Noise



- Source of noise: the discrete nature of radiation, i.e. the fact that each imaging system is recording an image by counting photons.
- This type of noise can be modeled as an independent additive noise which can be described by a zero-mean Gaussian.



Latest News Regarding Sensor Noise

- In September 2012 researchers showed that a better model for photon noise is color cameras is the Poisson distribution.
- The symmetry of the distribution depends on the mean value.
- Astronomers who often deal with weaker signals, have been using
 Poisson distribution to model the noise in telescope data.



Salt and Pepper Noise



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- A common form of noise is caused by data drop-out noise.
- It is also known as commonly referred to as intensity spikes, speckle or salt and pepper noise.

Sources of error:

- Errors in the data transmission.
- Burned pixels: the corrupted pixels are either set to the maximum value (which looks like snow in the image) or are set to zero ("peppered" appearance), or a combination of the two.
- Single bits are flipped over.
- Isolated/localized noise. It only affects individual pixels.

Filtering



Most of the images we capture are noisy.

Goal:



Mathematically, a filter H can be treated as a function on an input image I:

$$H(I) = R$$

Note: We use the terms *filter* and *transformation* interchangeably

Linear Transformation



A transformation H is **linear** if, for any inputs I₁(x,y) and I₂(x,y) (in our case input images), and for any constant scalar α we have:

$$H(\alpha I_1(x, y)) = \alpha H(I_1(x, y))$$

and

$$H(I_1(x, y) + I_2(x, y)) = H(I_1(x, y)) + H(I_2(x, y))$$

This means:

- Multiplication in the input corresponds to multiplication in the output
- Filtering an additive image is equivalent to filtering each image separately and then adding the results.

Shift-Invariant Transformation

A transformation H is shift-invariant if for every pair (x₀, y₀) and for every input image I(x,y), such that

$$H(I(x,y)) = R(x,y)$$

we get

$$H(I(x - x_0, y - y_0)) = R(x - x_0, y - y_0)$$

This means that the filter H does not change as we shift it in the image (as we move it from one position to the next).



Convolution



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- If a transformation (or filter) is linear shift-invariant (LSI) then one can apply it in a systematic manner over every pixel in the image.
- Convolution is the process through which we apply linear shift-invariant filters on an image.



Convolution is defined as:

$$R(x,y) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} H(x-i,y-j)I(i,j)$$

and is denoted as:

R = H * I

Another Look at Convolution



- Filtering often involves replacing the value of a pixel in the input image F with the weighted sum of its neighbors.
- Represent these weights as an image, H
- **H** is usually called the **kernel**
- The operation for computing this weighted sum is called convolution.

$$R = H * I$$

- Convolution is:
 - commutative, H * I = I * H
 - associative, $H_1^*(H_2^*I) = (H_1^*H_2)^*I$
 - distributive, $(H_1 + H_2) * I = (H_1 * I) + (H_2 * I)$

Smoothing via Simple Averaging



• One of the simplest filters is the mean filter: $H = \begin{bmatrix} \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \\ \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \\ \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \end{bmatrix}$

In this case,
$$R(x,y) = \sum_{i=-1}^{1} \sum_{j=-1}^{1} I(x-i, y-j)H(i,j)$$

It is used for removing image noise, i.e. for smoothing.





Original image

Image after mean filtering (25x25 kernel)



- Idea: Use a weighted average. Pixels closest to the central pixel are more heavily weighted.
- The Gaussian function has exactly that profile.
- Gaussian also better approximates the behavior of a defocused lens.



Isotropic Gaussian Filter

To build a filter H, whose weights resemble the Gaussian distribution, assign the weight values on the matrix H according to the Gaussian function:

$$H(i,j) = e^{-(i^2 + j^2)/2\sigma^2}$$

- Small σ, almost no effect, weights at neighboring points are negligible.
- Large σ, blurring, neighbors have almost the same weight as the central pixel.
- Commonly used σ values: Let w be the size of the kernel *H*. Then σ=w/5.
 For example for a 3x3 kernel, σ=3/5=0.6



 $H_{Gauss} = \begin{vmatrix} \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \\ \frac{1}{8} & \frac{1}{4} & \frac{1}{8} \\ \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \end{vmatrix}$

Gaussian Smoothing Example

Compared to mean filtering, Gaussian filtering exhibits no "ringing" effect.





"Ringing" effect





A close look at the frequency response of the two filters show that: compared to Gaussian filtering, mean filtering exhibits oscillations

The Effect of $\boldsymbol{\sigma}$



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Different σ values affect the amount of blurring, but also emphasize different characteristics of the image.





- The median filter considers each pixel in the image in turn and looks at its nearby neighbors to decide whether or not it is representative of its surroundings.
- It replaces a pixel value with the median of all pixel values in the neighborhood.
- It is a relatively slow filter, because it involves sorting.
- Can **not** be implemented via convolution.

Smoothing Example 1







Image after 9x9 Mean filtering

Original image



Image after 9x9 Gaussian filtering

Smoothing Example 2



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Original image corrupted by a zero mean Gaussian noise with $\sigma=8$. Image after 5x5 Mean filtering

Image after 5x5 Gaussian filtering

Mean Filter

Original image

Mean filtering

Mean filtering is sensitive to outliers.

It often causes a ringing effect.

It typically blurs edges.

Image after 7x7 Mean filtering

Image after applying 3 times 3x3 Mean filtering













Gaussian Filtering and Salt & Pepper Noise





Original image

Image with salt-pepper noise (1% prob. that a bit is flipped)

Image after 5x5

Gaussian filtering,

 $\sigma = 1.0$



Image after 9x9 Gaussian filtering, σ =2.0

- Gaussian filtering works very well for images affected by Gaussian noise
- It is not very effective in removing Salt and Pepper noise. Small σ values do not remove the Salt & Pepper noise, while large σ values blur the image too much.



Median Filtering and Salt & Pepper Noise



Original image

Image with salt-pepper noise (5% prob. that a bit is flipped)

Image after 3x3 Median filtering

Image after 7x7 Median filtering

Image after applying 3 times 3x3 Median filtering

- Median filtering preserves high spatial frequency details.
- It works well when less than half of the pixels in the smoothing window have been affected by noise.
- It is not very effective in removing Gaussian noise.

Image Sources



- 1. "Image with salt & pepper noise", Marko Meza.
- 2. The examples in slides 21-24 are courtesy of R. Fisher, S. Perkins, A. Walker and E. Wolfart
- 3. Some of the smoothing images are from the slides by D.A. Forsyth, University of Illinois at Urbana-Champaign.