



## Exercise 4: Random Sample Consensus (RANSAC)

Model estimations on noisy data are usually error-prone. Even a small number of outliers will influence the estimation such that the resulting model can produce large errors. The goal is to identify models that minimize the error and ignore outliers.

### 1 Theory

RANSAC assumes that a model built with a minimum number of data points for this model does not contain outliers. If we imagine the minimum number of points for a line, the generated line will exactly fit through those two points. To consider every point the model error is evaluated on the whole data set. In a scenario where we expect the majority of the data points to be in a valid range we can use this strategy to find a model fitting the inliers and ignoring the outliers.

#### RANSAC algorithm

1. Determine the minimum number  $n_{mdl}$  of data points required to build the model
2. For  $n_{it}$  iterations do
  - (a) Choose randomly  $n_{mdl}$  points out of your data to estimate the model
  - (b) Determine the error of the current model using all data points
3. Choose model with lowest error

We have to consider the probability  $P_{corr}$  how likely it is to pick the  $n_{mdl}$  right points for an optimal model in  $n_{it}$  iterations at least once. Knowing the relative frequency  $p_o$  for outliers we can compute the number of required iterations by

$$n_{it} = \left\lceil \frac{\log(1 - P_{corr})}{\log(1 - (1 - p_o)^{n_{mdl}})} \right\rceil \quad (1)$$

### 2 Implementation tasks

We will implement a RANSAC algorithm to fit a line through a point plot. Therefore, we assume to obtain sample points on a line where outliers occur due to measurement errors. Complete the gaps in *lineransac.m*

1. Implement this algorithm in the function *commonransac* in a common way not only related to line fitting (see function interface for details).

2. Implement the function *fitline* to estimate the line parameters
3. Now think of a proper error function to evaluate the current model on the whole data set and implement it in the function *lineerror*

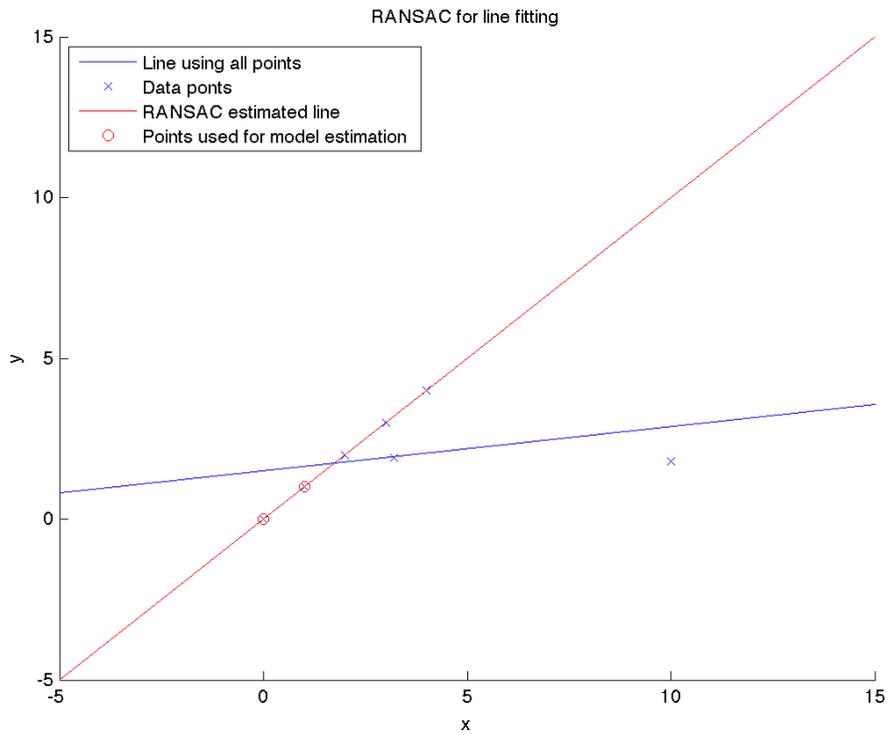


Figure 1: RANSAC for line fitting

Some useful matlab functions: `randperm`, `pinv`, `norm`